

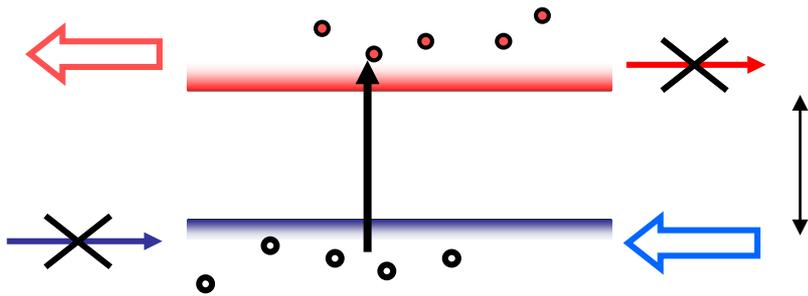


NETWORK SCHOOL

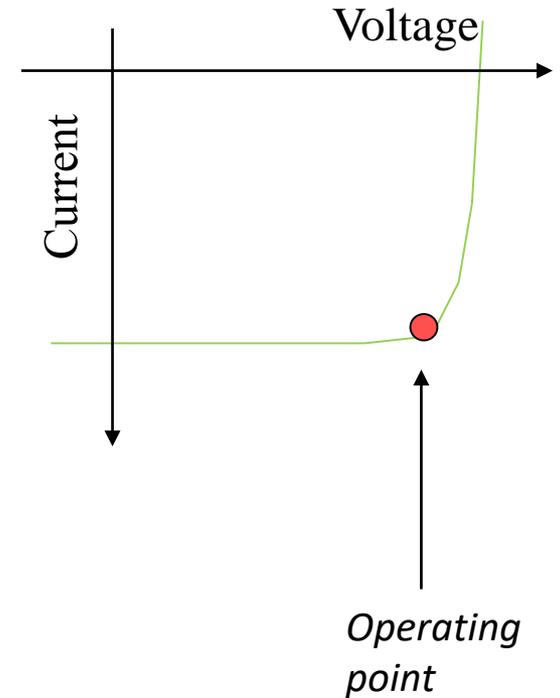
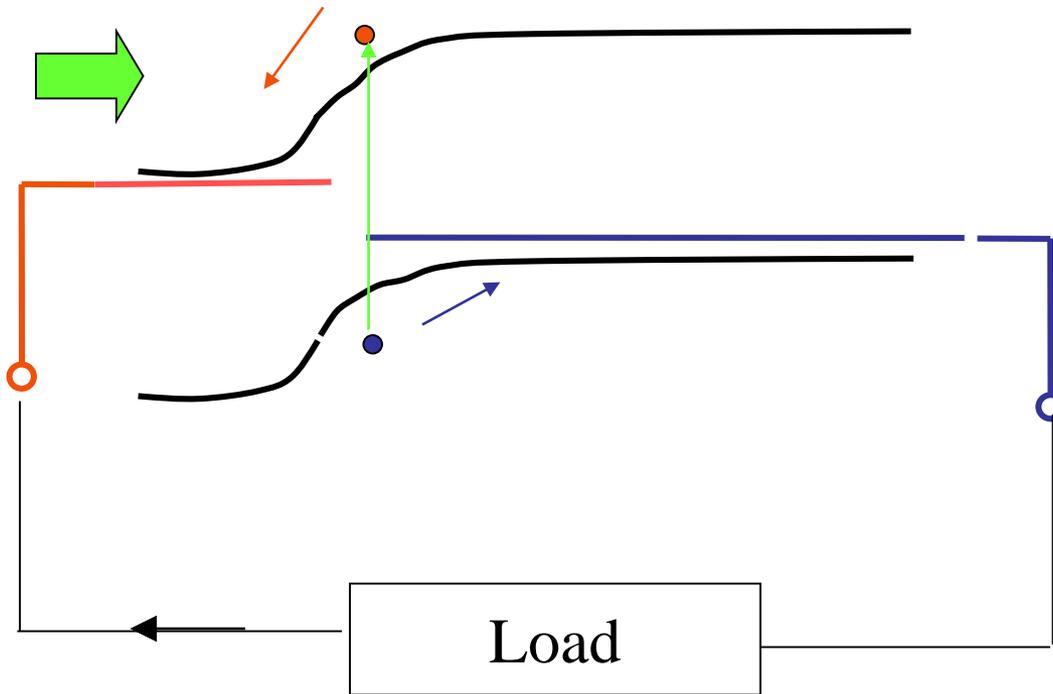
10th April 2019

Device scale simulation of organic photovoltaic devices

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- PV generation requires:
 - photon **absorption** across an energy gap
 - **separation** of photogenerated charges
 - **asymmetric contacts** to an external circuit

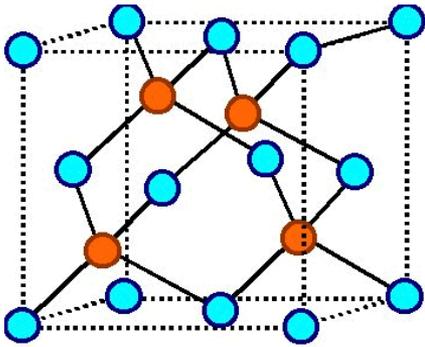


Operating: photovoltage x photocurrent = electric power

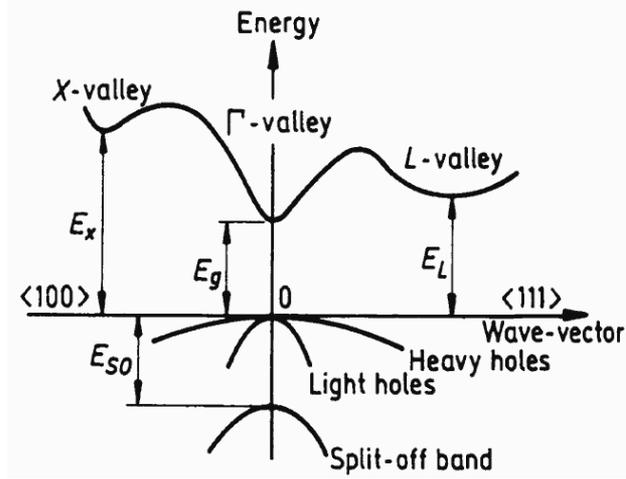
Outline

- **Basics of solar cell device modelling**
- What is different about organic solar cells
- Device modelling approaches to OPV
- Case studies: steady state models
- Transient modelling

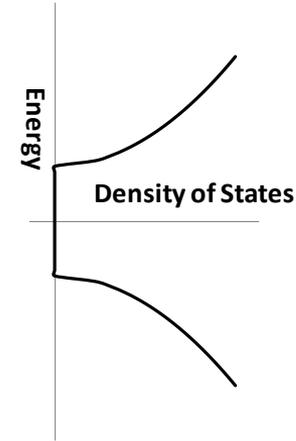
Semiconductors



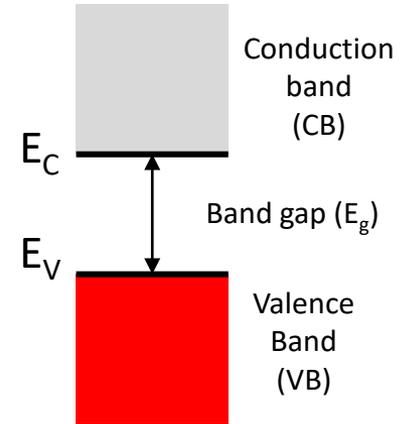
Crystal structure



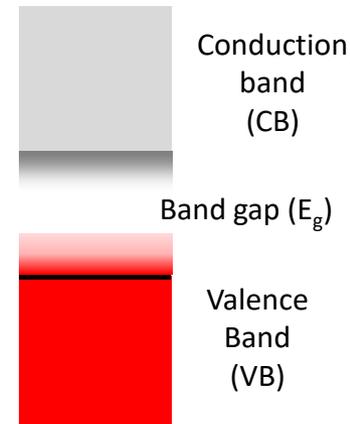
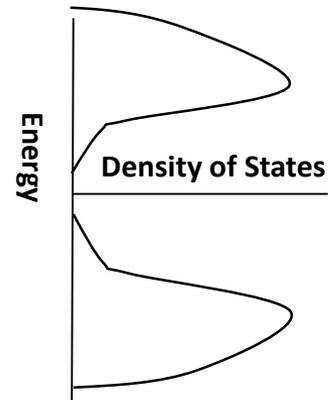
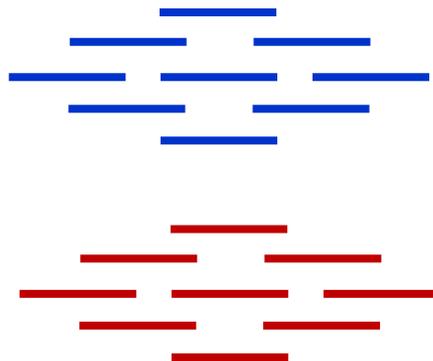
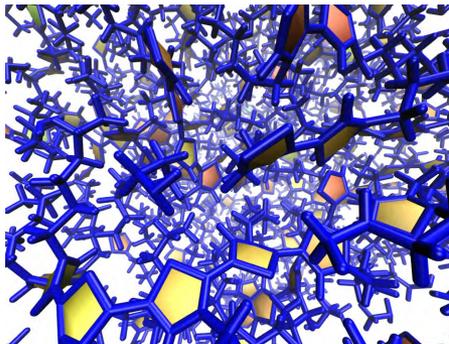
Band structure



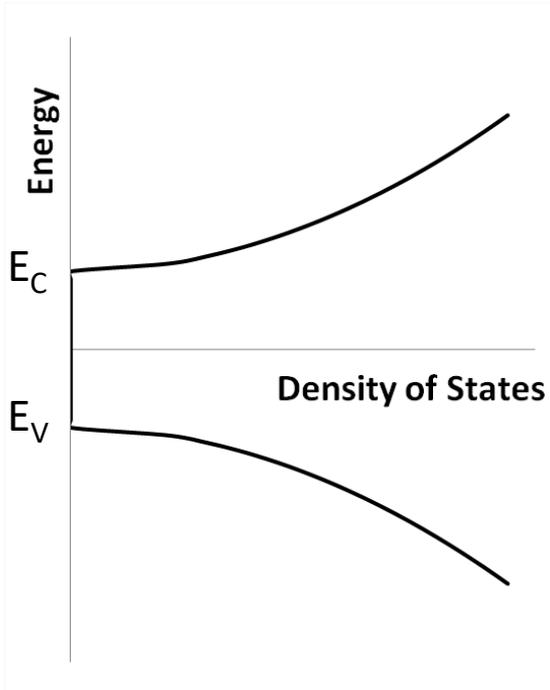
Density of States



Band picture

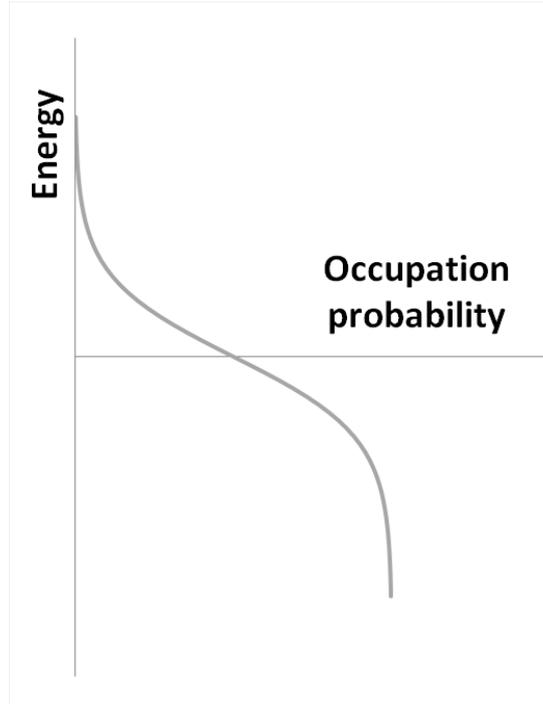


Charge carrier statistics



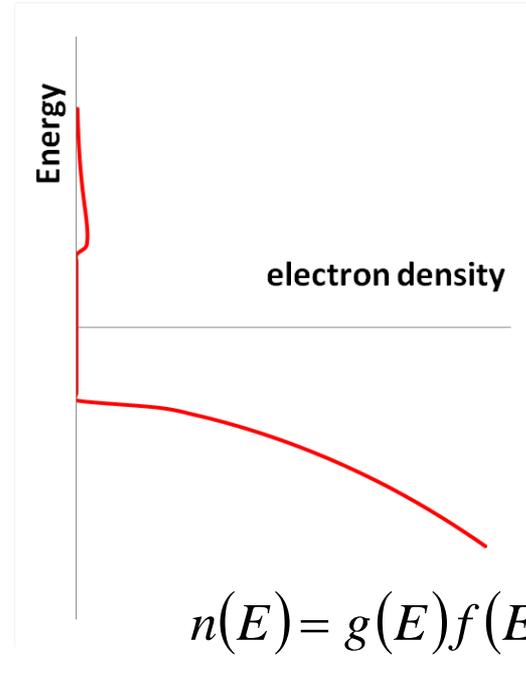
$$g(E)$$

Density of states for electrons and holes



$$f(E) = \frac{1}{\exp\left(-\frac{E - E_F}{kT}\right) + 1}$$

Charge carrier populations follow **Fermi Dirac statistics**



$$n(E) = g(E)f(E)$$

$$n = \int_{E_C}^{\infty} g(E)f(E)dE \quad n = \exp\left(-\frac{E_C - E_F}{kT}\right)N_C$$

$$p = \int_{-\infty}^{E_V} g(E)(1 - f(E))dE$$

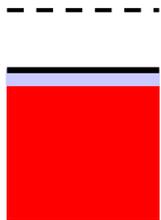
$$p = \exp\left(-\frac{E_F - E_V}{kT}\right)N_V$$

Total concentrations of free electrons and holes

Fermi levels and Doping: at equilibrium



$$n = N_C e^{-(E_C - E_F)/kT}$$



$$p = N_V e^{-(E_F - E_V)/kT}$$

$$np = n_i^2 = N_C N_V e^{-E_g/kT}$$

Intrinsic semiconductor:
equal concentrations of
free electrons and holes



$$n \approx N_D$$



$$p \approx n_i^2 / N_D$$

$$E_F = E_C - kT \ln N_C + kT \ln N_D$$

n doped semiconductor: High
density of free electrons
introduced by impurity atoms
that have one too many
valence electrons



$$n \approx n_i^2 / N_A$$



$$p \approx N_A$$

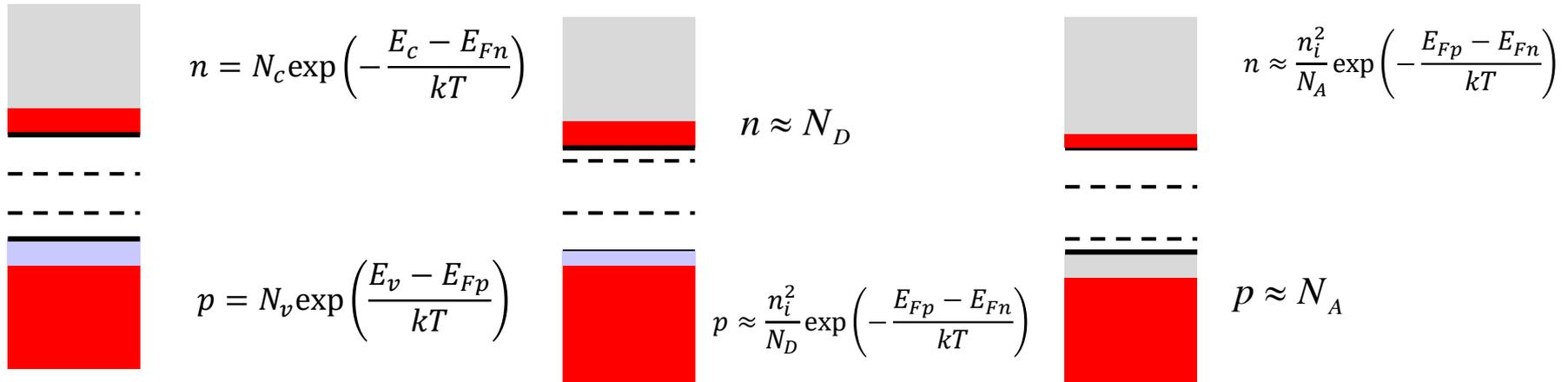
$$E_F = E_V + kT \ln N_V - kT \ln N_A$$

p doped semiconductor:
High density of free holes
introduced by impurity
atoms that have one too
few valence electrons

Fermi levels are *pinned*

Fermi levels and Doping: under bias

Optical or electrical bias increases the concentrations of free electrons and / or holes



$$E_{F_n} > E_{F_p}$$

$$np = n_i^2 e^{(E_{F_n} - E_{F_p})/kT}$$

$$E_{F_n} \approx E_c - kT \ln N_c + kT \ln N_D$$

$$E_{F_p} < E_{F_n}$$

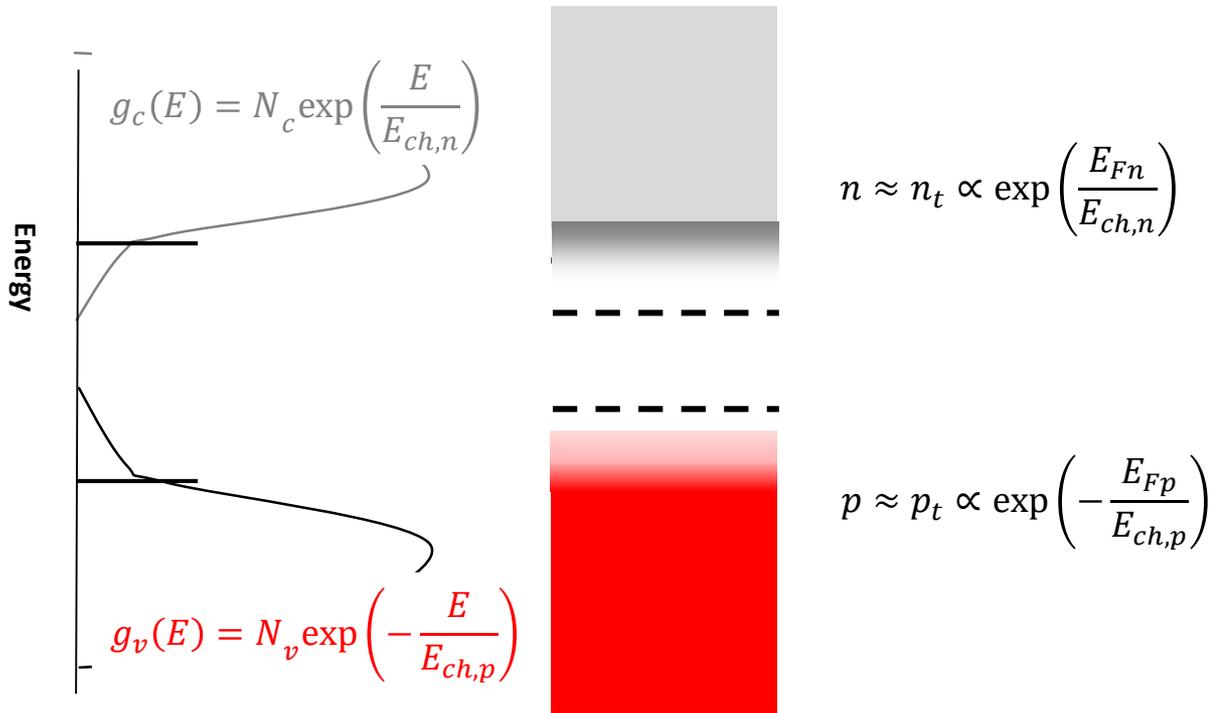
$$E_{F_n} > E_{F_p}$$

$$E_{F_p} = E_v + kT \ln N_v - kT \ln N_A$$

Charge carrier populations are assumed to be in **quasi thermal equilibrium**

This is valid if the rate of scattering within a band is faster than the rate of relaxation between bands (Boltzmann relaxation time approximation)

Fermi levels : with tail states

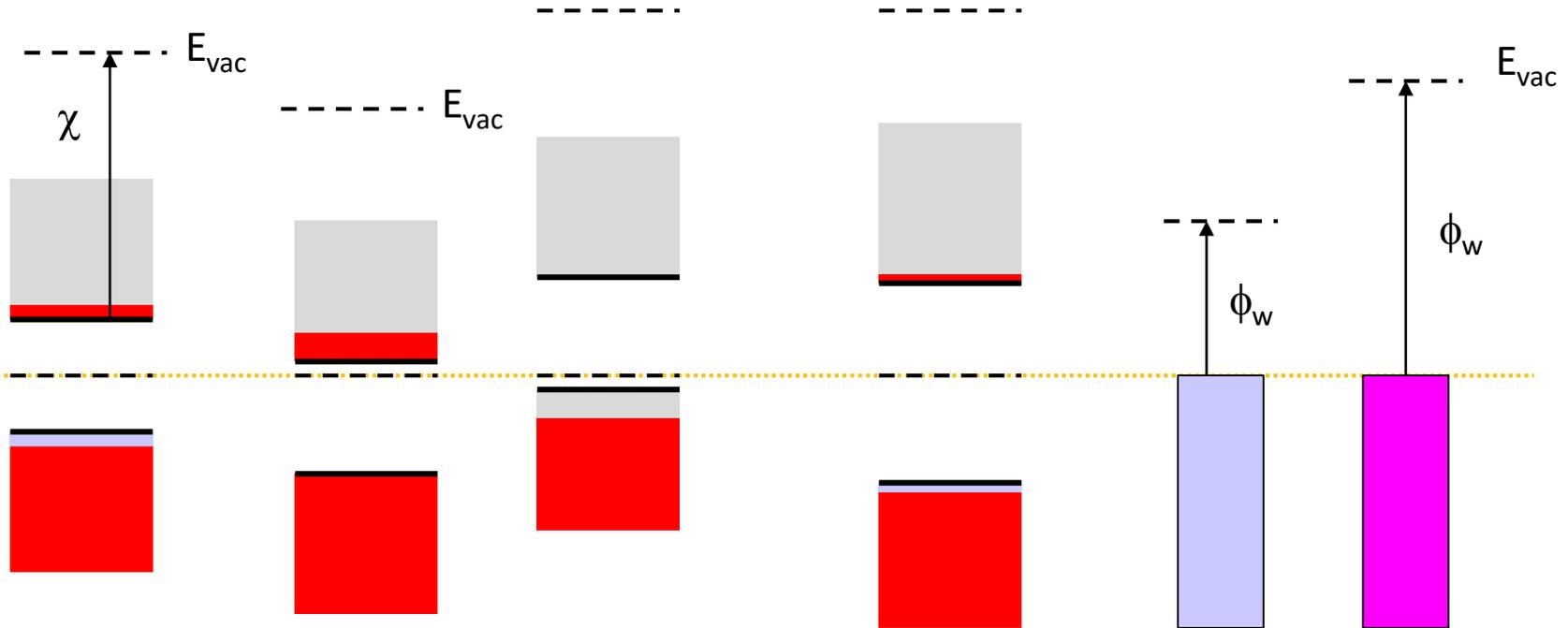


Symmetric case:

$$np \propto \exp\left(\frac{E_{Fn} - E_{Fp}}{E_{ch}}\right) \quad n \propto \exp\left(\frac{qV}{2E_{ch}}\right)$$

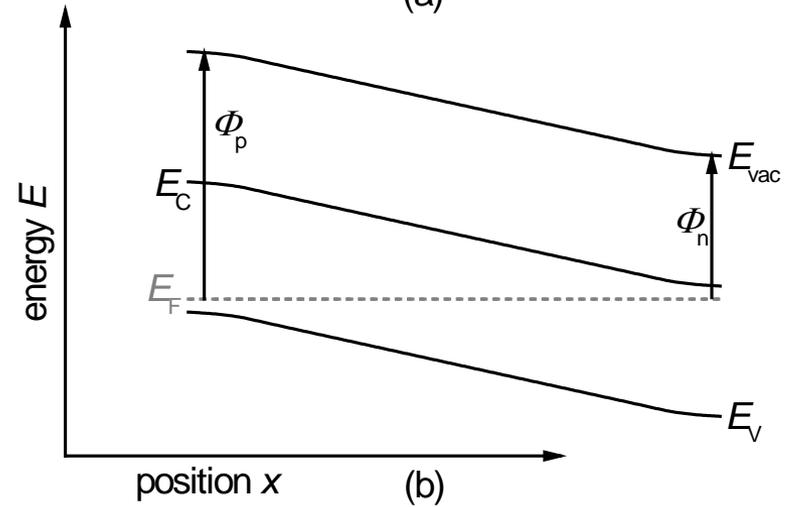
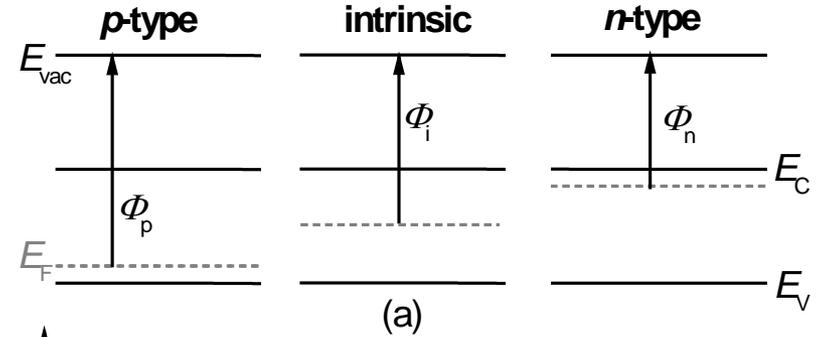
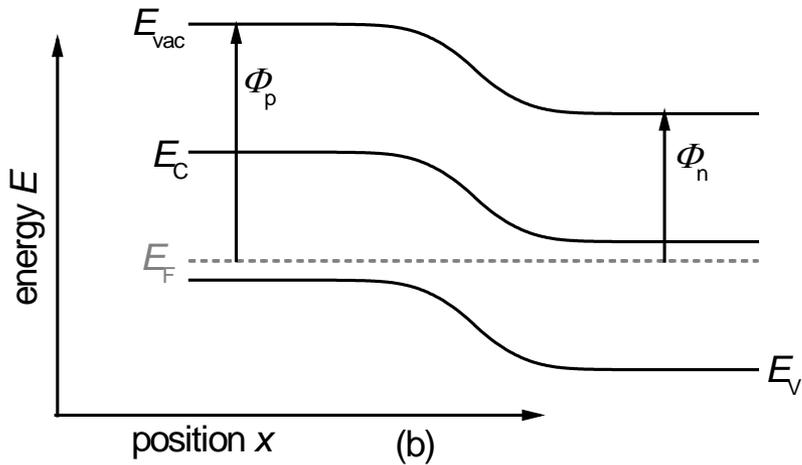
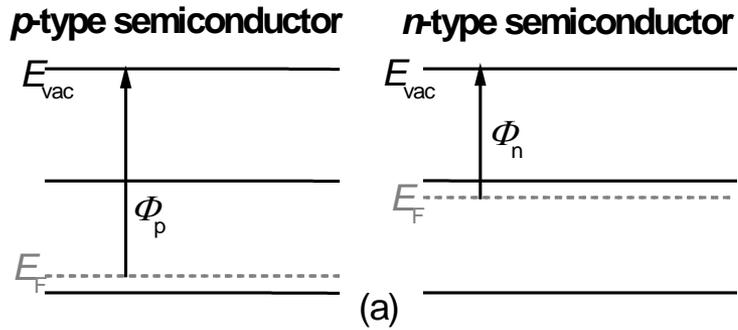
- Typically assume a common quasi Fermi level for all electrons (or holes) in tail states
- May have same or different quasi Fermi level for free charges

Alignment



- The Fermi level in equilibrium controls band alignment
- Fermi level position is influenced by band gap, doping and electron affinity (or work function)

Band profiles for p-n and p-i-n devices in equilibrium



- Band alignment at boundaries controlled by boundary conditions
- Fermi level constant
- Poisson's equation determines band profile

Photogeneration

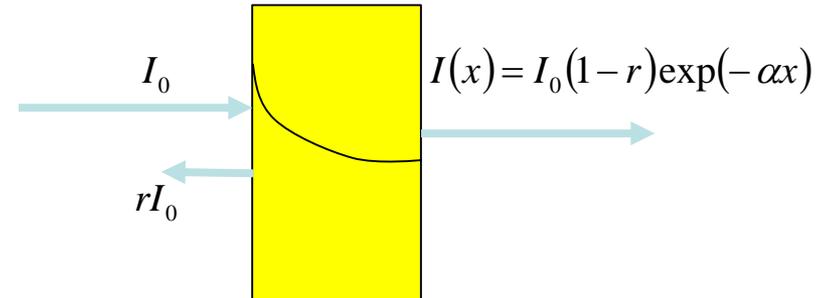
Light absorption in the semiconductor increases electron and hole densities above their equilibrium values

Attenuation of light intensity:

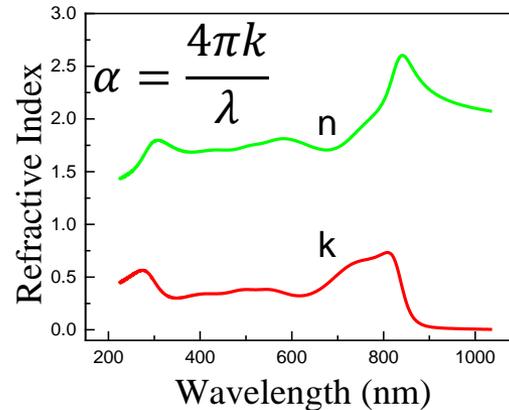
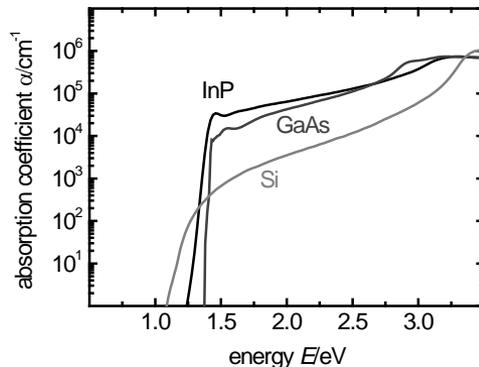
Simple model: Beer Lambert law

Electron-hole pair *generation rate*

$$G(E, x) = L(E, x) = \alpha(E)b_s(E)(1 - r(E)) \exp\left(\int_0^x \alpha(E)dx'\right)$$



Absorption spectrum $\alpha(E)$



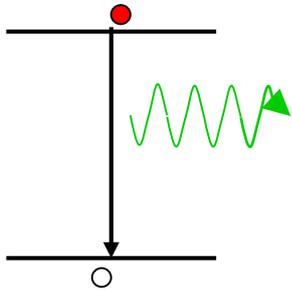
Advanced model: Solve transfer matrix equation using (n,k) data for layers

- In inorganic semiconductors assume generation rate is equal to photon absorption rate $G(E, x) = L(E, x)$. In general, $G = P_{CS}L$

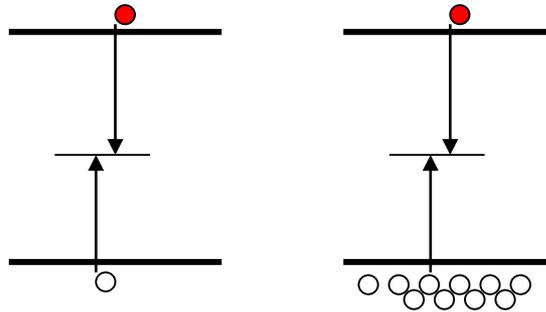
Recombination

Excess electrons and holes recombine

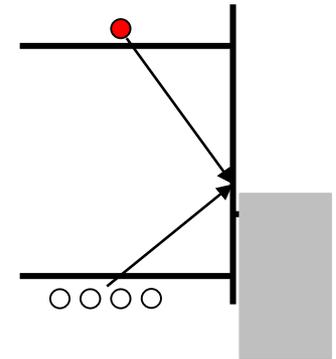
Radiative



Non-radiative (Shockley-Read Hall)



Surface



$$R_{rad} = B_{rad} (np - n_i^2) \\ \propto (e^{eV/kT} - 1)$$

$$R_{SRH} = \frac{np - n_i^2}{(n + n_t)\tau_p + (p + p_t)\tau_n}$$

$$R_{SRH} = \frac{n - n_0}{\tau_n}$$

$$R \propto (e^{eV/2kT} - 1)$$

$$R \propto (e^{eV/kT} - 1)$$

$$J_n(x_{surf}) = eS_n(n - n_0)$$

$$R \propto (e^{eV/kT} - 1)$$

- When tail states or traps are present, distinguish recombination between free or trapped electrons or holes; trapped charge likely to dominate

- $R_{SRH} = R_{SRH}(n_{free}, p_{trapped}) + R_{SRH}(n_{trapped}, p_{free}) + R_{SRH}(n_{free}, p_{free})$

Current generation

Excess electrons and holes can drive a current

- Electron and hole current densities are defined from the quasi Fermi level gradient

$$J_n(\mathbf{r}) = \mu_n n \nabla_{\mathbf{r}} E_{F_n}$$

$$J_p(\mathbf{r}) = \mu_p p \nabla_{\mathbf{r}} E_{F_p}$$

$$J(\mathbf{r}) = J_n(\mathbf{r}) + J_p(\mathbf{r})$$

- Fermi level gradient due to gradient in carrier density, electrostatic potential, band edge energy and density of states (We assume no gradient in Temperature .)

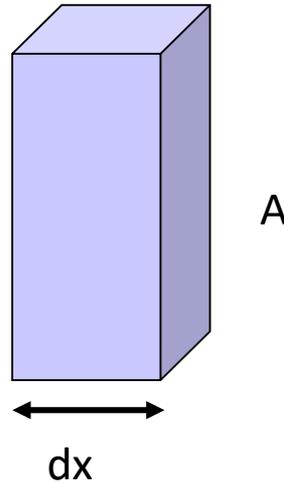
$$J_n(\mathbf{r}) = eD_n \nabla n + q\mu_n n (F - \nabla \chi - kT \nabla \ln N_c) \quad J_p(\mathbf{r}) = -eD_p \nabla p + q\mu_p p (F - \nabla \chi - \nabla E_g + kT \nabla \ln N_v)$$

- For a uniform material, current densities J are more commonly written as the sum of drift and diffusion terms

$$J_n(\mathbf{r}) = eD_n \nabla n + e\mu_n F n$$

$$J_p(\mathbf{r}) = -eD_p \nabla p + e\mu_p F p$$

Book keeping



In volume $A \cdot dx$ in unit time,

No electrons being generated – no. electrons recombining = no electrons leaving – no electrons entering

$$G \cdot A dx$$

$$R \cdot A dx$$

$$-\frac{1}{e} J_n(x+dx) A$$

$$-\frac{1}{e} J_n(x) A$$

$$G - R = -\frac{1}{e} \frac{dJ_n}{dx}$$

Semiconductor device equations in steady state

Continuity:
$$-\frac{1}{e} \frac{dJ_n}{dx} = G - R \qquad \frac{1}{e} \frac{dJ_p}{dx} = G - R$$
 Any gradient in current density is matched by Generation – Recombination

Current:

electrons:
$$J_n = eD_n \frac{dn}{dx} + en\mu_n F \quad \Rightarrow \quad J_n = en\mu_n \frac{dE_{F_n}}{dx}$$

holes:
$$J_p = -eD_p \frac{dp}{dx} + ep\mu_p F \quad \Rightarrow \quad J_p = ep\mu_p \frac{dE_{F_p}}{dx}$$

Poisson's equation:
$$\frac{d^2\phi_i}{dx^2} = \frac{e}{\epsilon_r \epsilon_0} (N_a - N_d + n - p)$$
 Charges arrange to minimise electrostatic potential energy

\Rightarrow set of 3 differential equations, for n , p and ϕ_i .

Plus: boundary conditions at the electrodes, e.g.

$$J_n(x_{surf}) = eS_n(n - n_0)$$

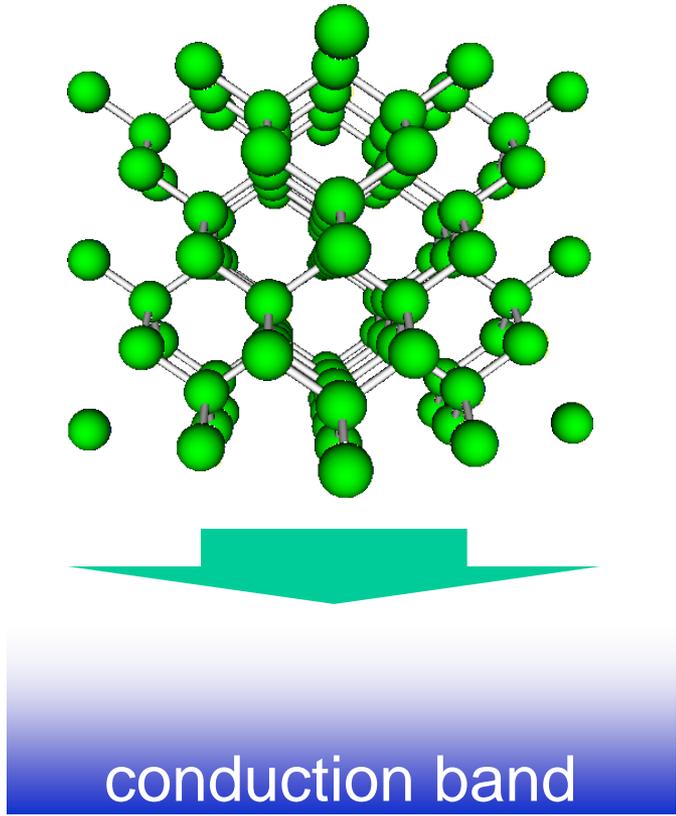
$$\phi(x_{front}) - \phi(x_{rear}) = V$$

Outline

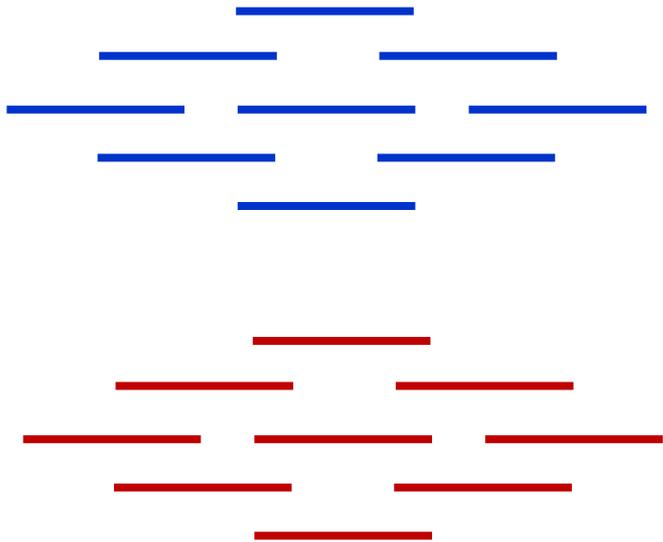
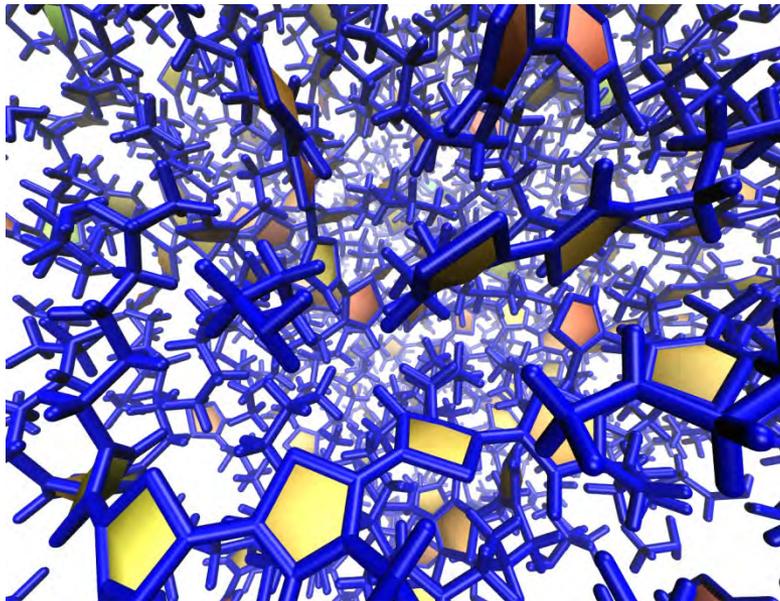
- Basics of solar cell device modelling
- **What is different about organic solar cells**
- Device modelling approaches to OPV
- Case studies: steady state models
- Transient device modelling

Inorganic vs. organic semiconductor: Density of States

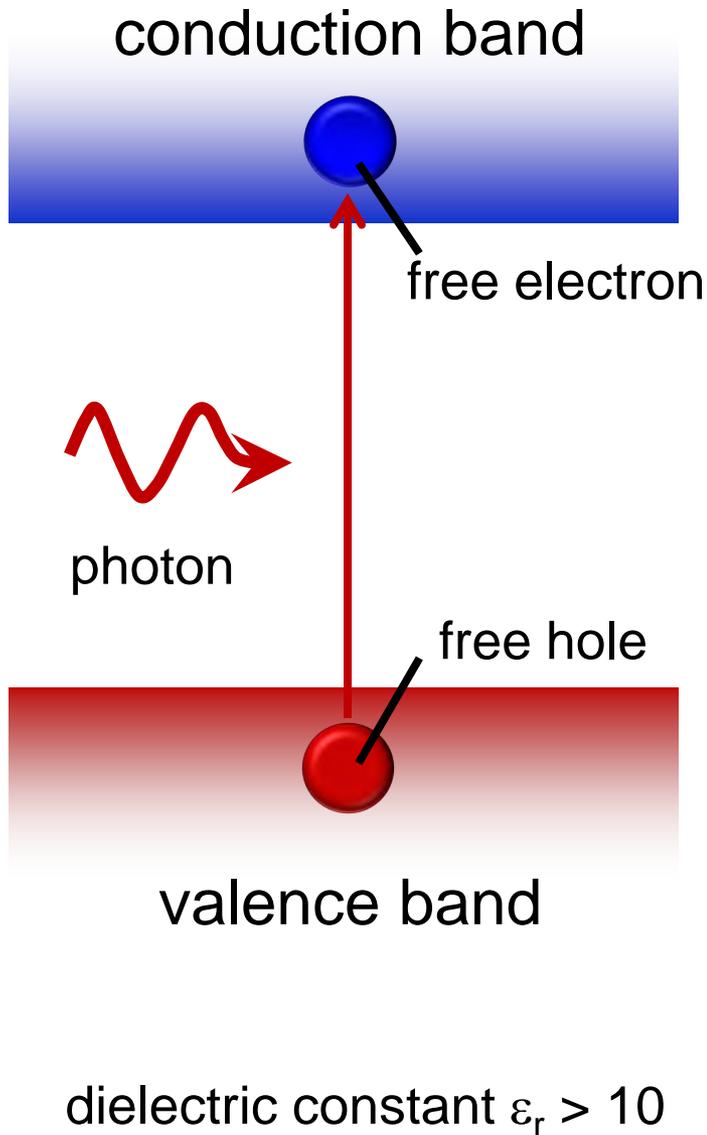
<http://www.iue.tuwien.ac.at/phd/hoessinger/node26.html>



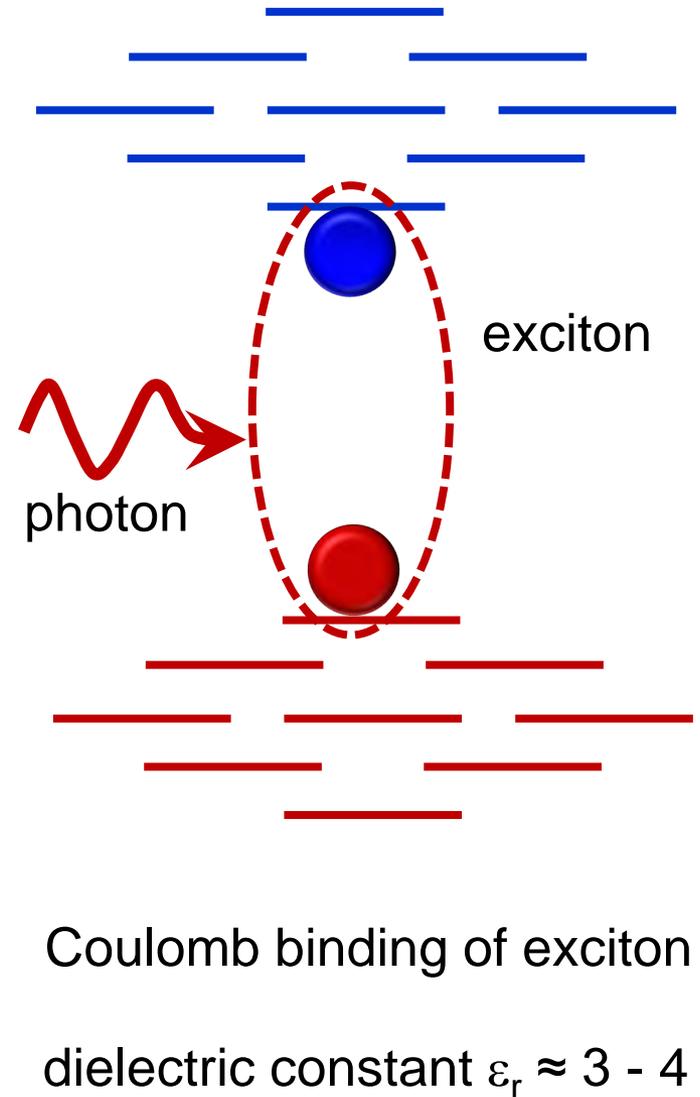
inorganic
organic



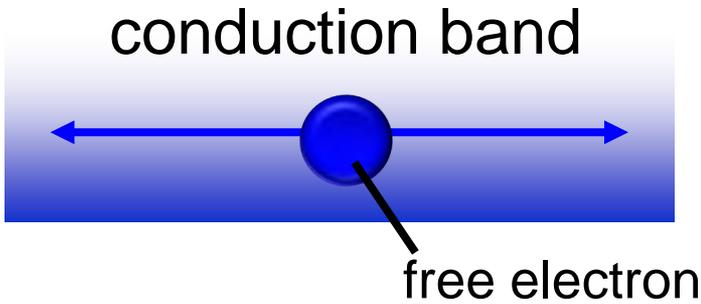
Photoexcitation in inorganic vs. organic semiconductors



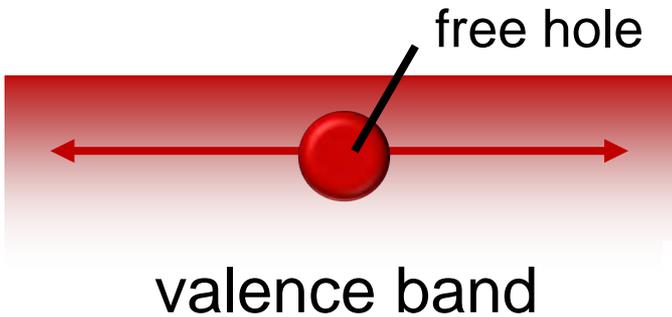
inorganic
organic



Transport in inorganic vs. organic semiconductors

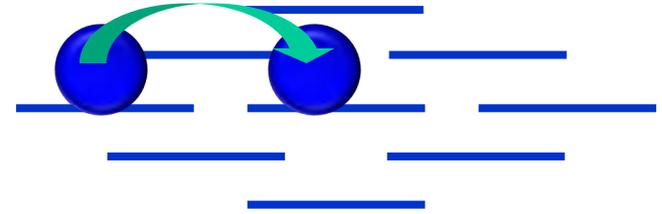


mobility:
 $\mu = 1 \text{ to } 10^4 \text{ cm}^2/\text{Vs}$

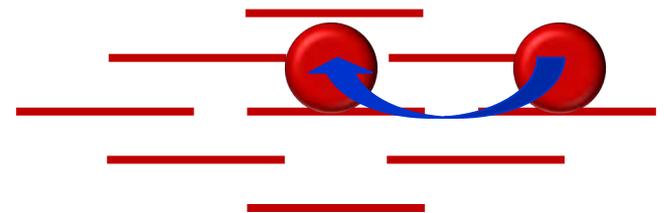


Band transport: D_n, μ_n are constant

inorganic



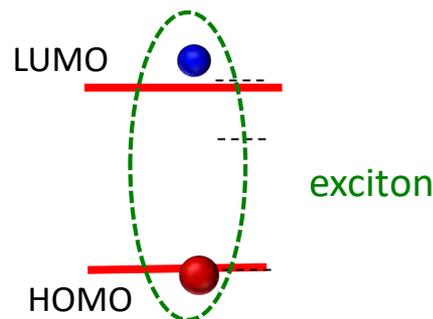
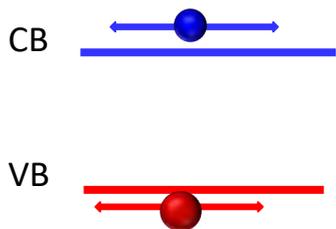
mobility:
 $\mu \approx 10^{-4} \text{ cm}^2/\text{Vs}$



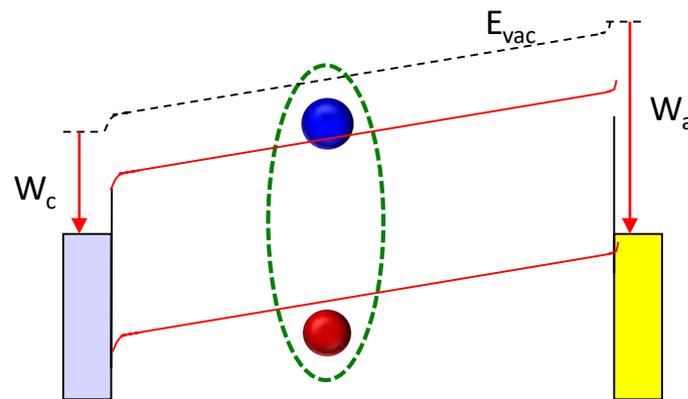
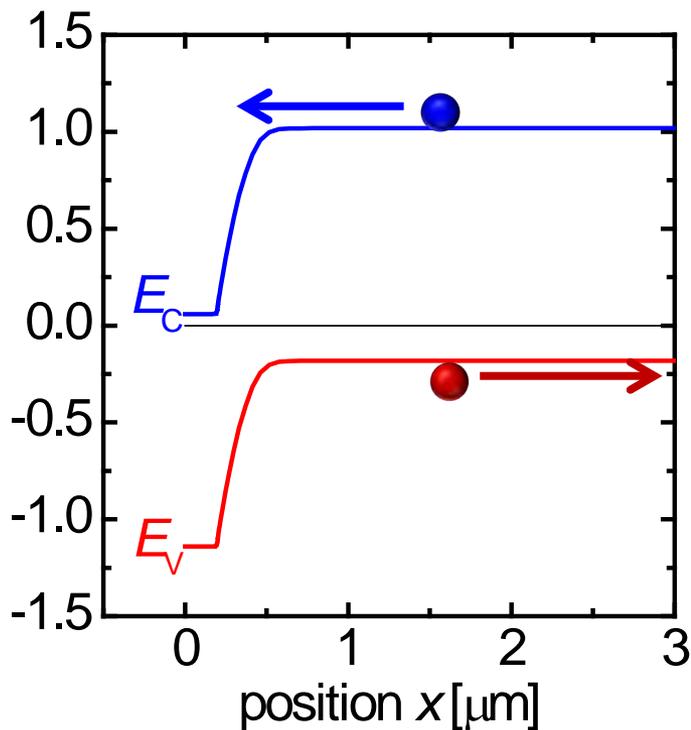
Hopping: D_n, μ_n are n dependent

$$J_n = eD_n \frac{dn}{dx} + en\mu_n F$$

Photocurrent generation in inorganic vs. organic solar cells



inorganic
organic



e.g. using a pn-junction

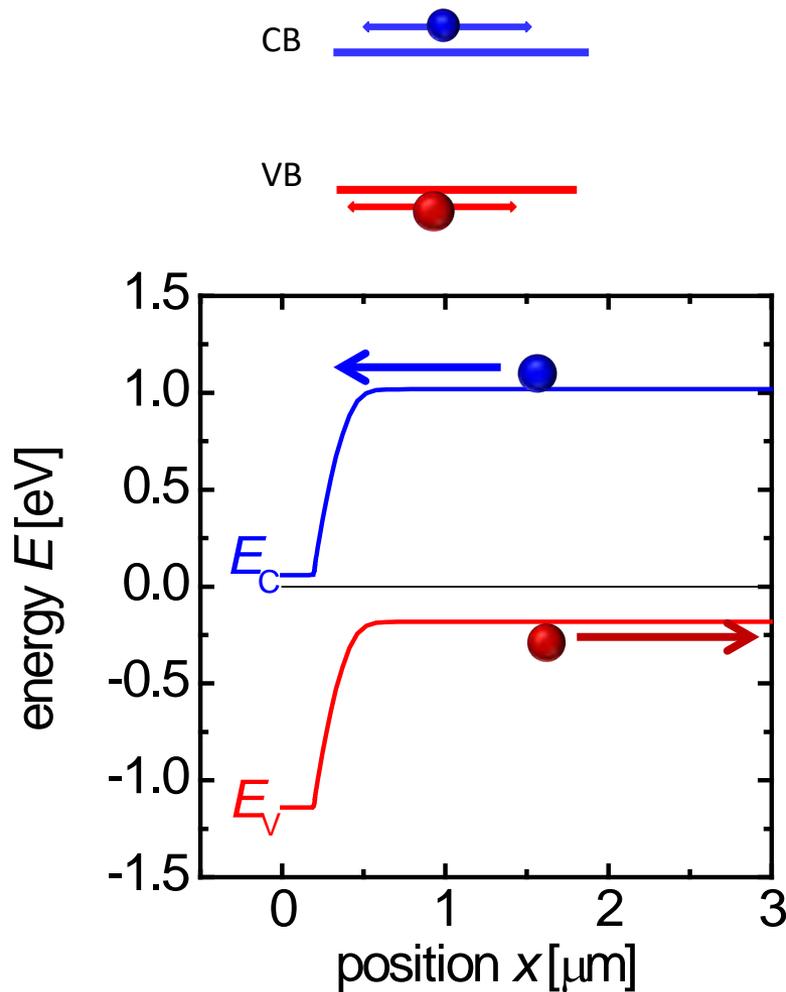
$$G(E, x) = L(E, x)$$

e.g. using a MIM junction

$$G(E, x) = P_{cs} L(E, x)$$

$$P_{cs} \ll 1$$

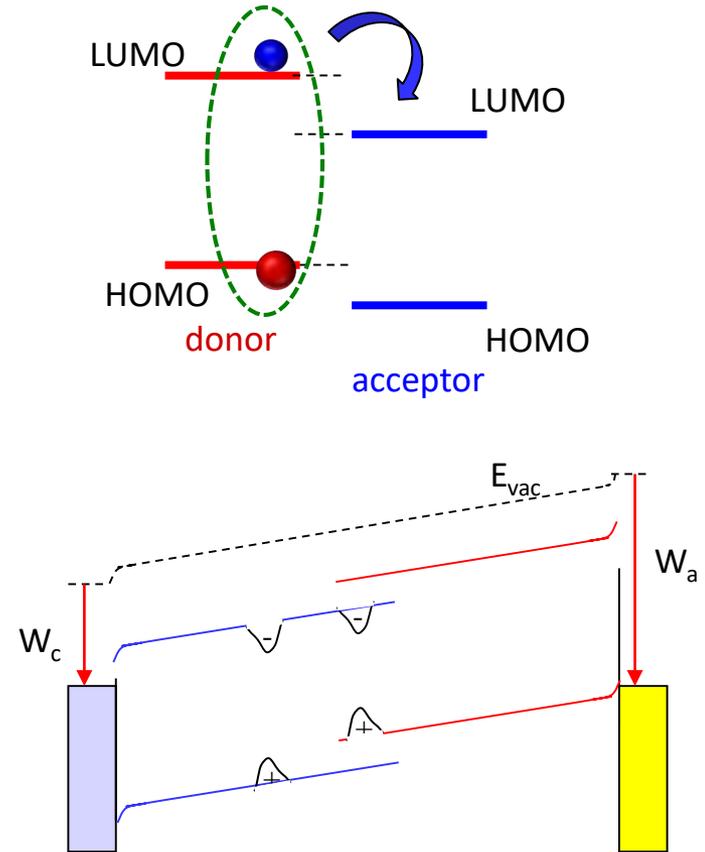
Photocurrent generation in inorganic vs. organic solar cells



e.g. using a pn-junction

inorganic

organic

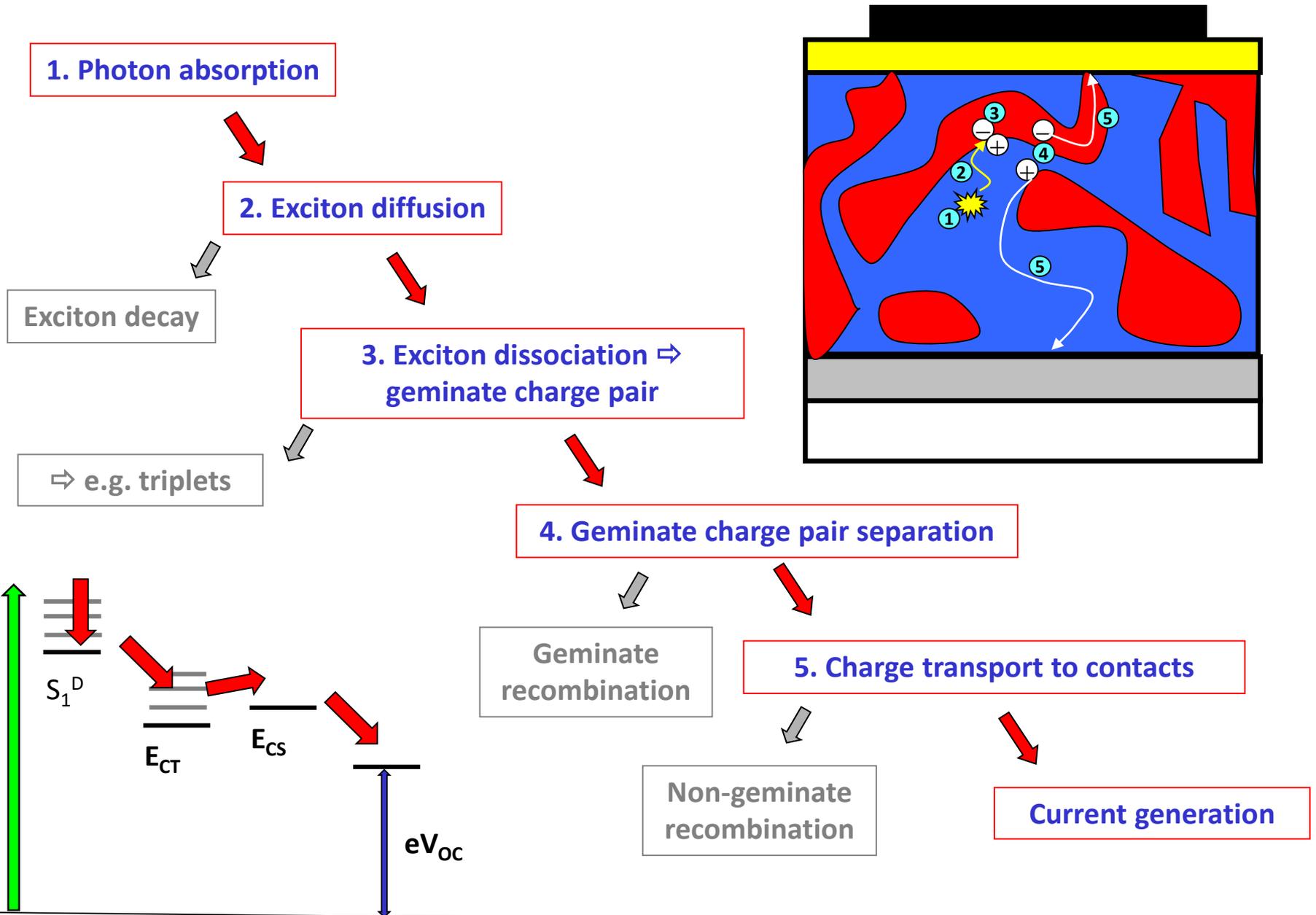


using a planar or bulk heterojunction

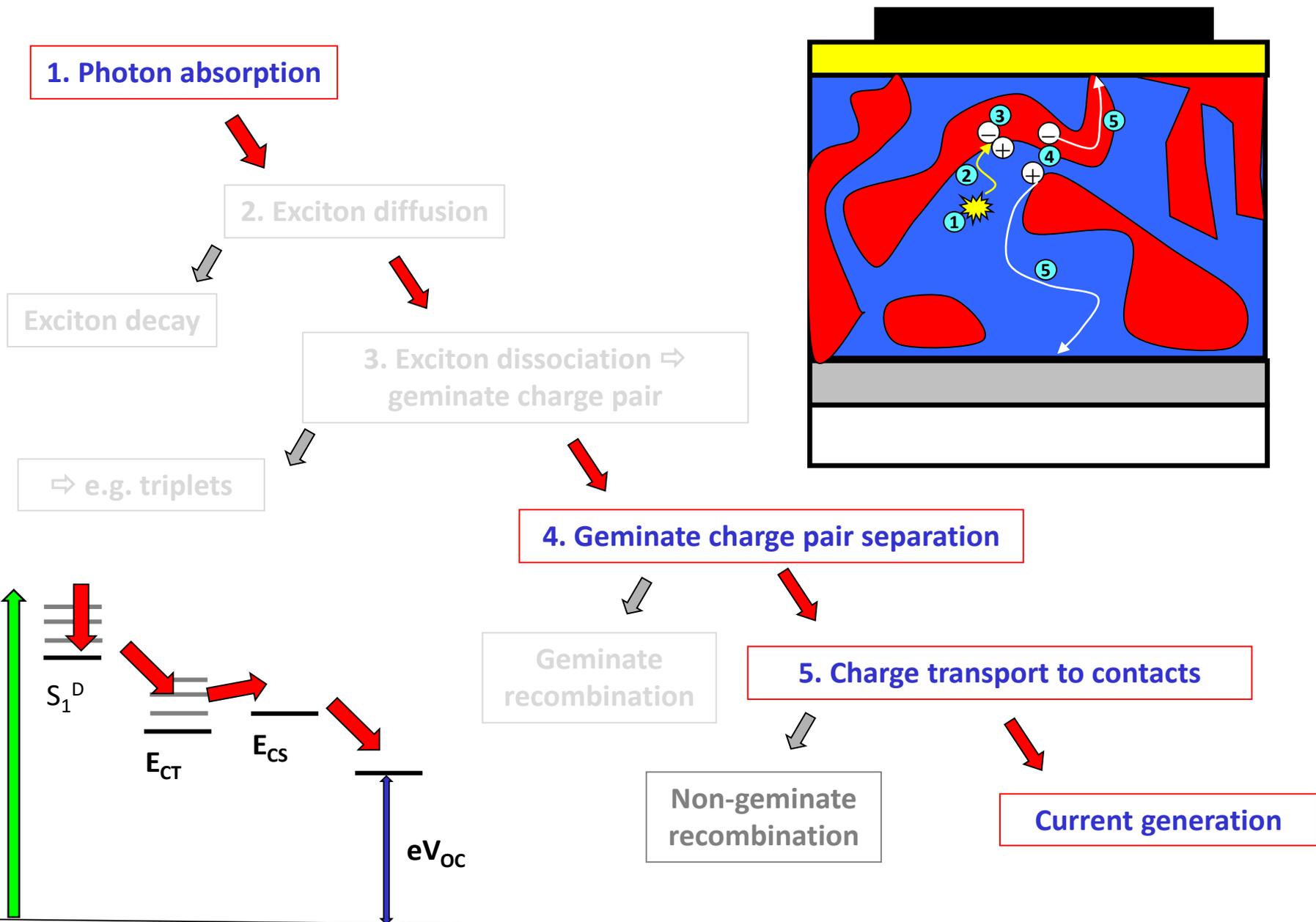
$$G(E, x) = P_{CS} L(E, x)$$

$$P_{CS} < \sim 1$$

Key steps in OPV device function

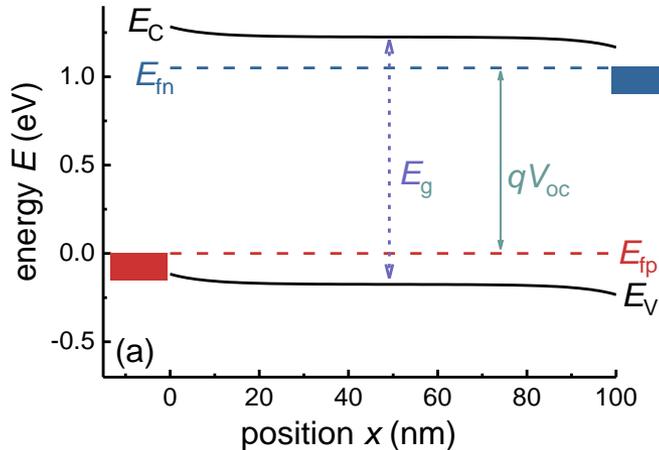


Processes captured with a device scale model

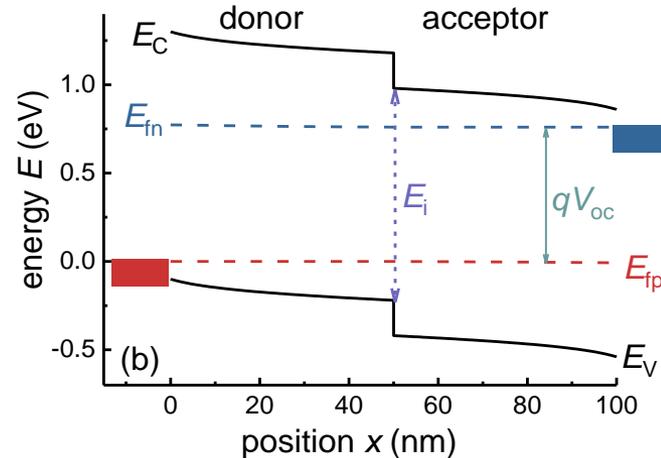


Dealing with the bulk heterojunction: Effective medium

Homojunction (MIM structure)

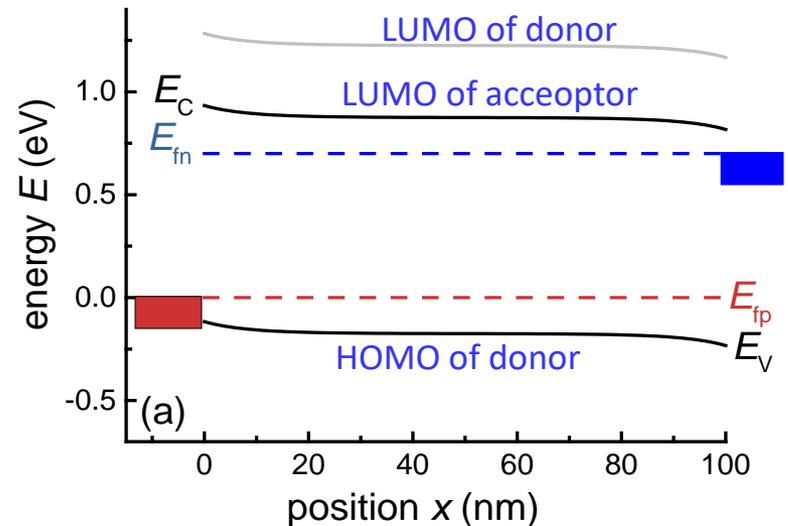


Planar heterojunction



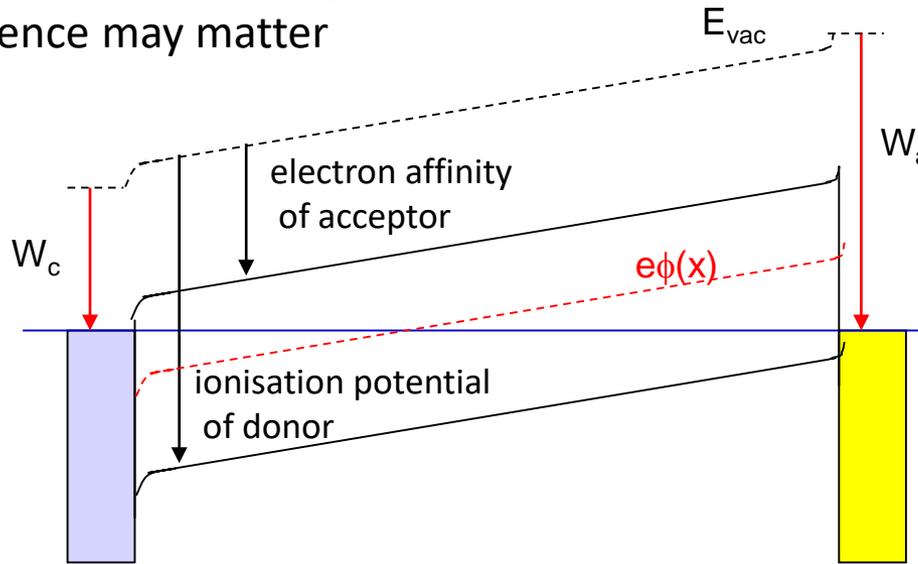
- Active layer is an effective semiconductor medium with conduction band energy at LUMO of acceptor and valence band at HOMO of donor
- Charge dynamics and electrostatics within active layer described by same coupled partial differential equations and boundary conditions... except coefficients may not be constant!

Bulk heterojunction



Device Physics of Organic Solar Cell: What's different?

Semiconductor layer is thin: optical interference may matter



Material is energetically disordered: DoS extends into gap

Material not (intentionally) doped (so rely on electrodes for photocurrent direction)

$$-\frac{1}{e} \frac{dJ_n}{dx} = G - R$$

$$J_n = eD_n \frac{dn}{dx} + en\mu_n F$$

$$\frac{dF}{dx} = \frac{e\rho(x)}{\epsilon_0 \epsilon_r}$$

Generation is not well understood

Lifetime, mobility and diffusion are not constant

ϵ_r is small (3-4)

Outline

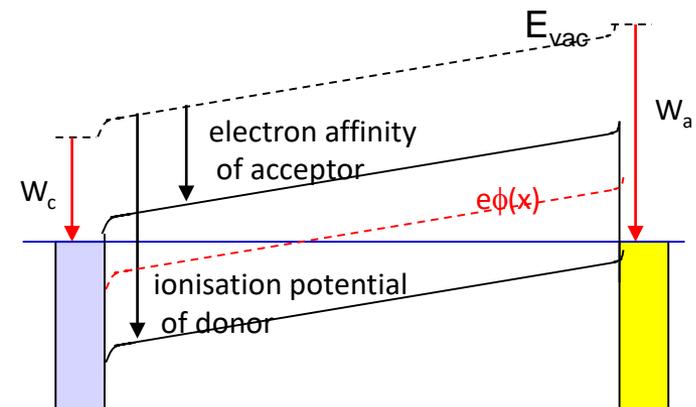
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Common approach to OPV device physics

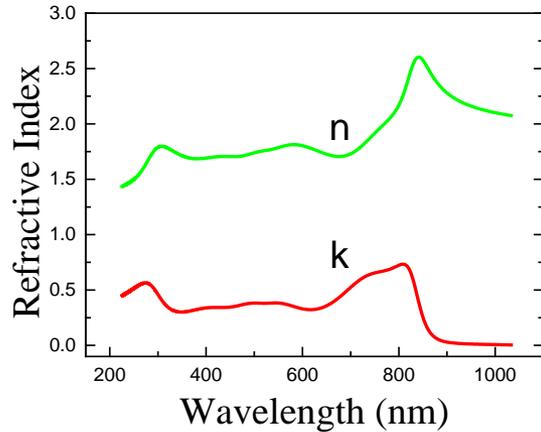
- Use **effective medium** for photoactive layer,
- **Undoped** /lightly doped active layer, metallic electrodes, doped interlayers possible
- Parabolic density of states in conduction and valence bands, possibly with discrete deep **traps** and / **or tail states**
- **Quasi thermal equilibrium** assumed (commonly)
- Transfer matrix, Beer Lambert or uniform generation
- Empirical formula to **relate pair generation to photon absorption** (often $P_{cs} = 1$)
- Only charge carriers above band edges are mobile; makes average mobility dependent on total charge density
- Uniform free carrier (or “band”) mobility
- **Shockley Read Hall recombination** statistics (distinguishing trapped and free carriers) and recombination at electrode interfaces

Implement DE solver in MATLAB or other code;
Use commercial software

(most simulations in this talk done with ASA)

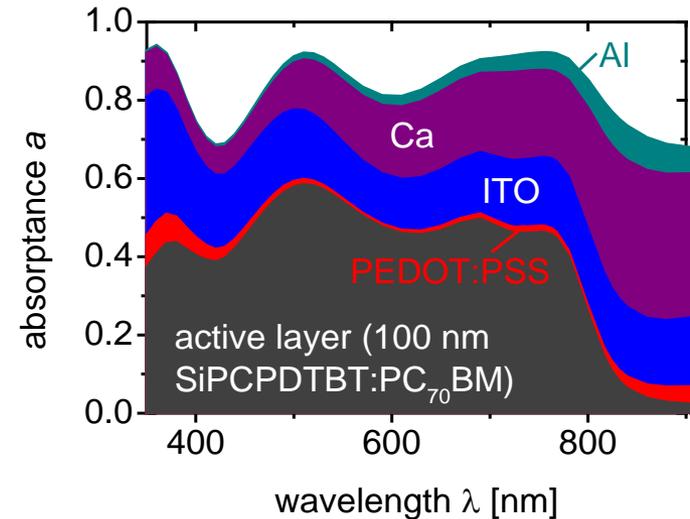
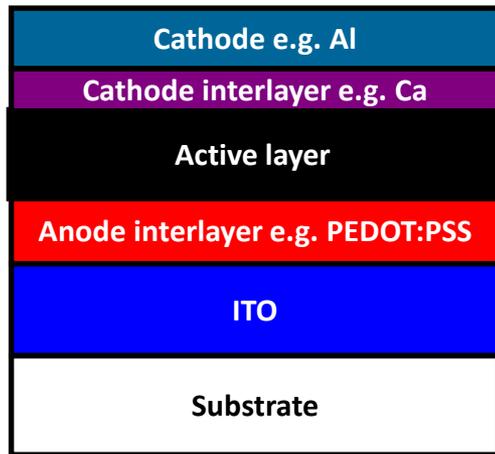


Device simulation input: Optical absorption



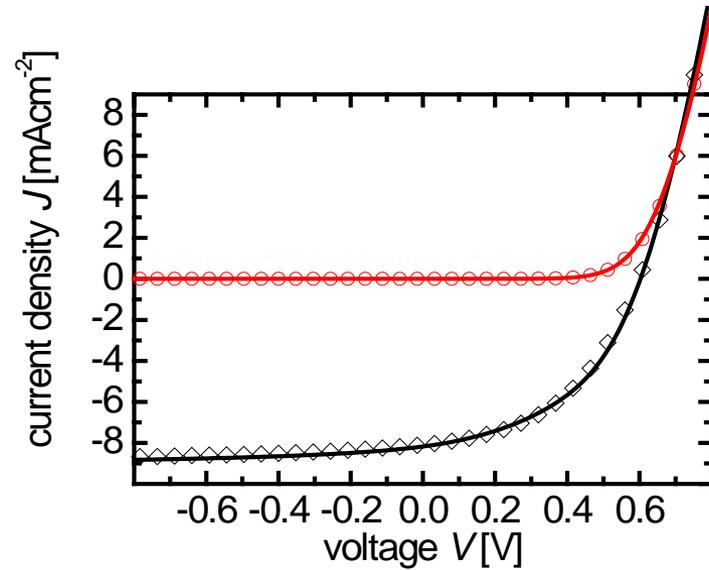
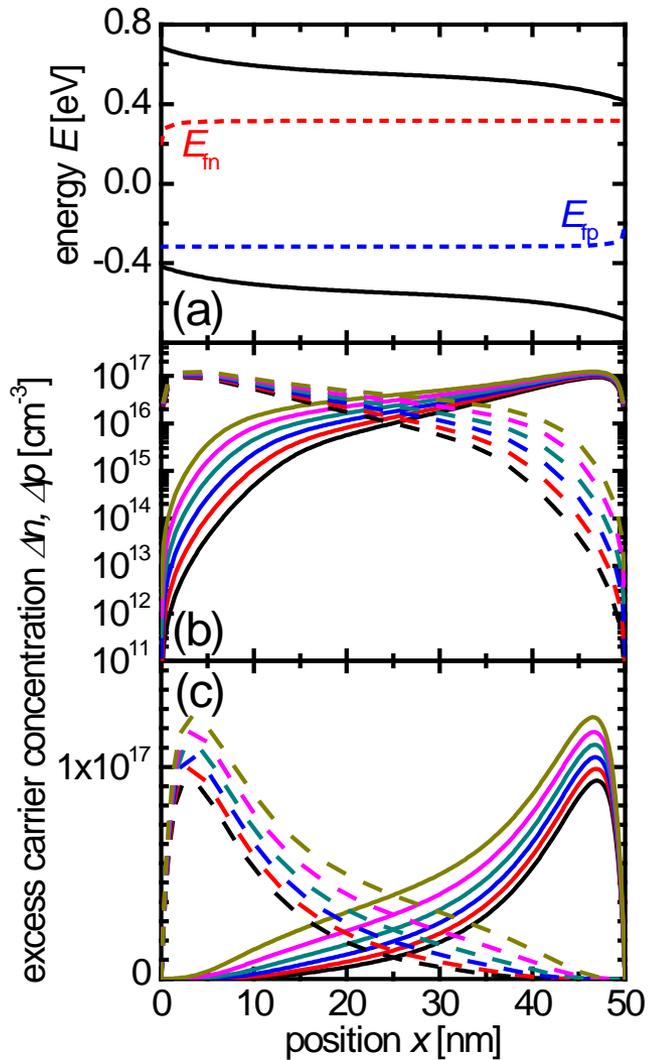
- Layer thicknesses comparable to wavelength of light so use optical model

Transfer Matrix Model



- Tune layer thicknesses to maximise absorbance A in the active layer

Device simulation output: Band profiles, charge density and J-V curves

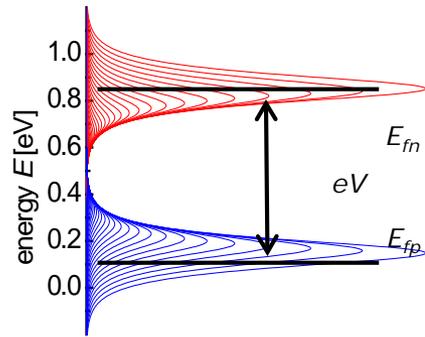


- Spatial variation of n and p mean that zero-dimensional models of recombination are often not accurate

Device simulation output: Tail state filling and ideality factor

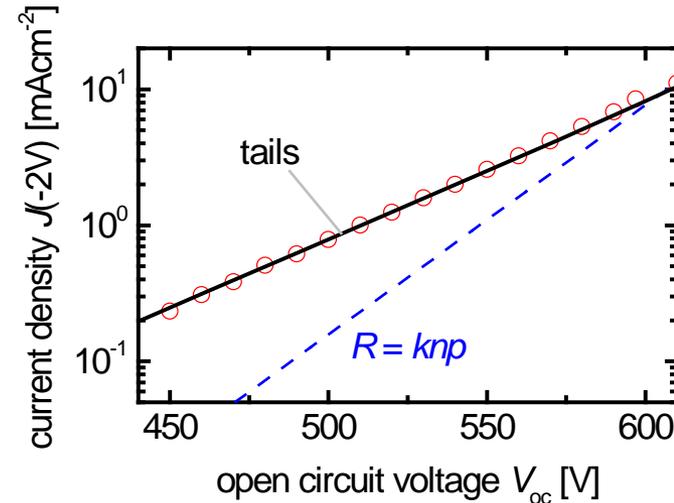
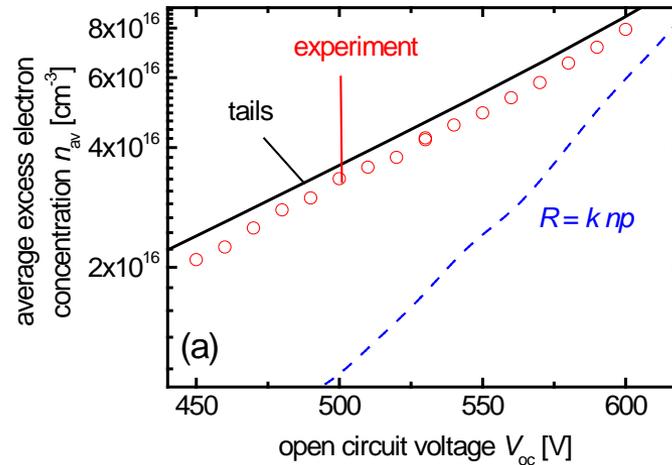
- Band tails can be represented as exponential or Gaussian functions
- Shockley Read Hall recombination via tails (free to trapped charges)
- Charge carrier density as a function of Voc strongly reflects the role of tail states
- Ideality factor indicates recombination mechanism (free to trapped charge)

T. Kirchartz et al, Phys. Rev. B (2011)



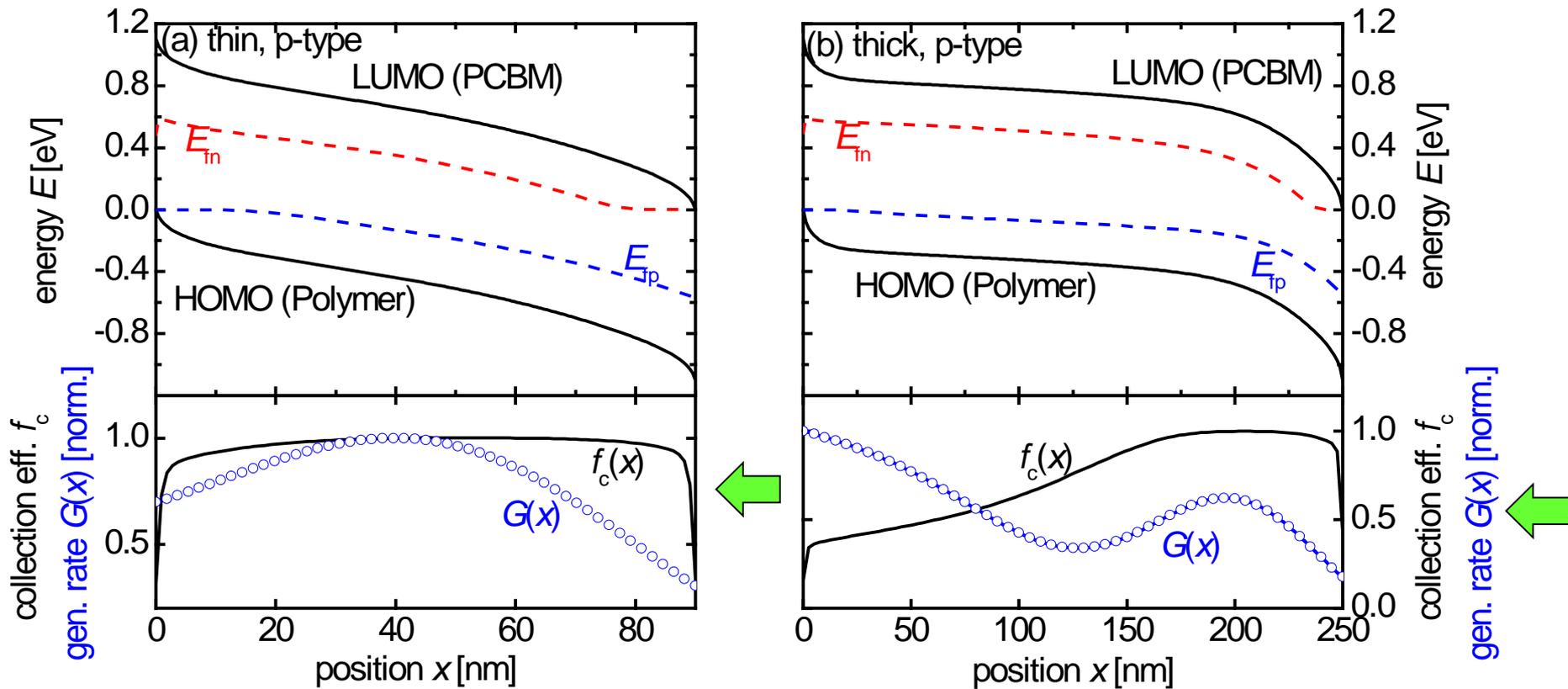
$$DOS \propto \exp\left(\frac{E}{E_{ch}}\right)$$

$$n \propto \exp\left(\frac{eV}{2E_{ch}}\right)$$



$$R = kn_f p_t = kn_0 p_0 \exp\left(\frac{qV}{2kT} + \frac{qV}{2E_{ch}}\right)$$

Device simulation : Generation and recombination profiles



Efficient charge carrier collection needs a high built-in electric field!

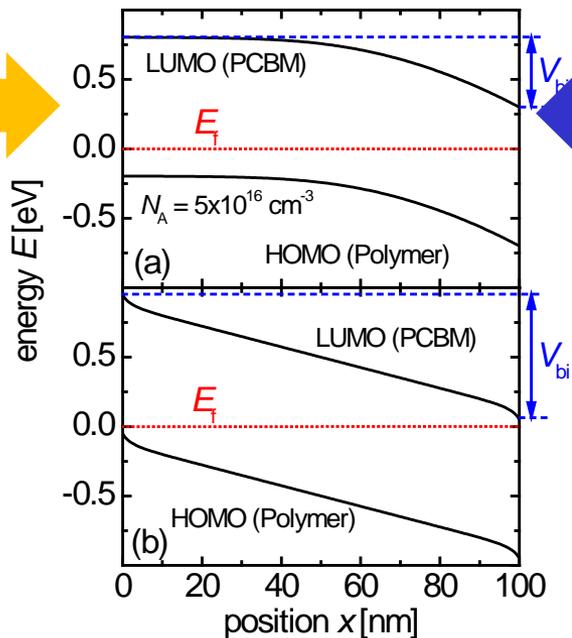
How should things change to account for spin?

- Use **effective medium** for photoactive layer,
- **Undoped** /lightly doped active layer, metallic electrodes, doped interlayers possible
 - **Spin dependent injection?**
- Parabolic density of states in conduction and valence bands, possibly with discrete deep **traps** and / **or tail states**
- **Quasi thermal equilibrium** assumed (commonly)
- Transfer matrix, Beer Lambert or uniform generation
- **Empirical formula to relate pair generation to photon absorption:**
 - Accounting for ISC, singlet and triplet diffusion to interfaces
 - Accounting for spin dependence of exciton dissociation and charge separation
- Only charge carriers above band edges are mobile; makes average mobility dependent on total charge density
- Uniform free carrier (or “band”) mobility
 - **Spin dependence of charge transfer and transport**
- **Shockley Read Hall recombination** statistics (distinguishing trapped and free carriers) and recombination at electrode interfaces
 - **Spin dependence of trapping and detrapping**
 - **Spin dependence of pair combination**
 - **Spin dependence of CT state to ground transition**

Outline

- Basics of solar cell device modelling
- What is different about organic solar cells
- Device modelling approaches to OPV
- **Case studies: steady state models**
- Transient device modelling

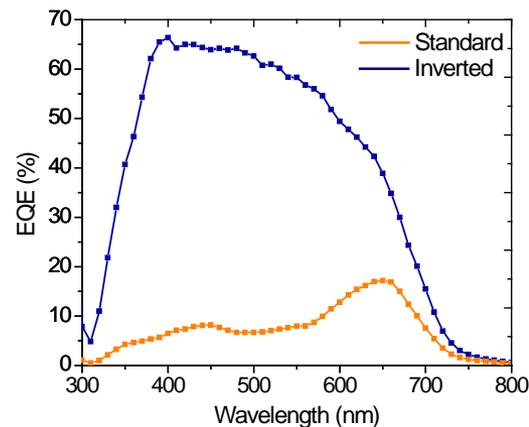
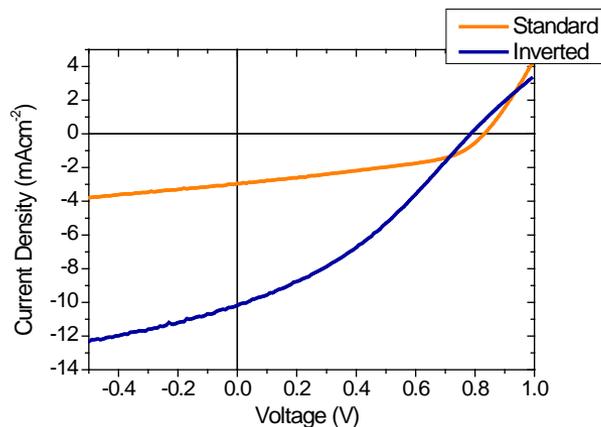
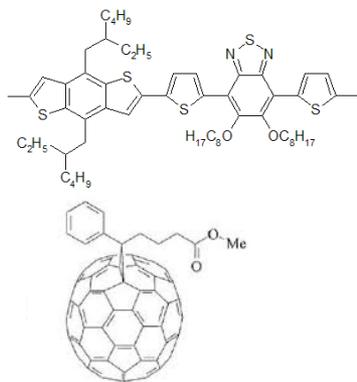
Case study I: Effect of unintentional doping



Equilibrium band profile influenced by doping: doping limits extent of field bearing region

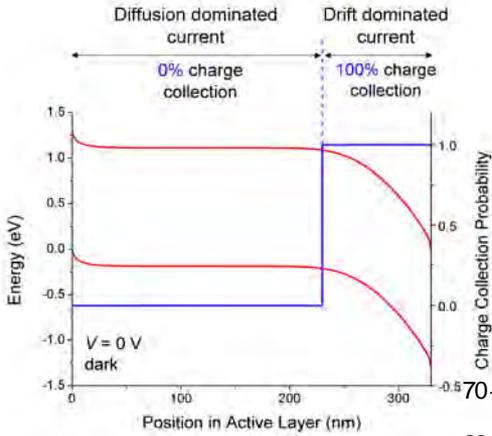
- When mobility is low, field needed for efficient charge collection

- Example:** polymer:PC70BM solar cells with unintentional p doping of 10^{16} cm^{-3}



ITO/PEDOT:PSS/OPV-32:PC₇₁BM/Ca/Al
ITO/ZnO/OPV-32:PC₇₁BM/PEDOT:PSS/Ag

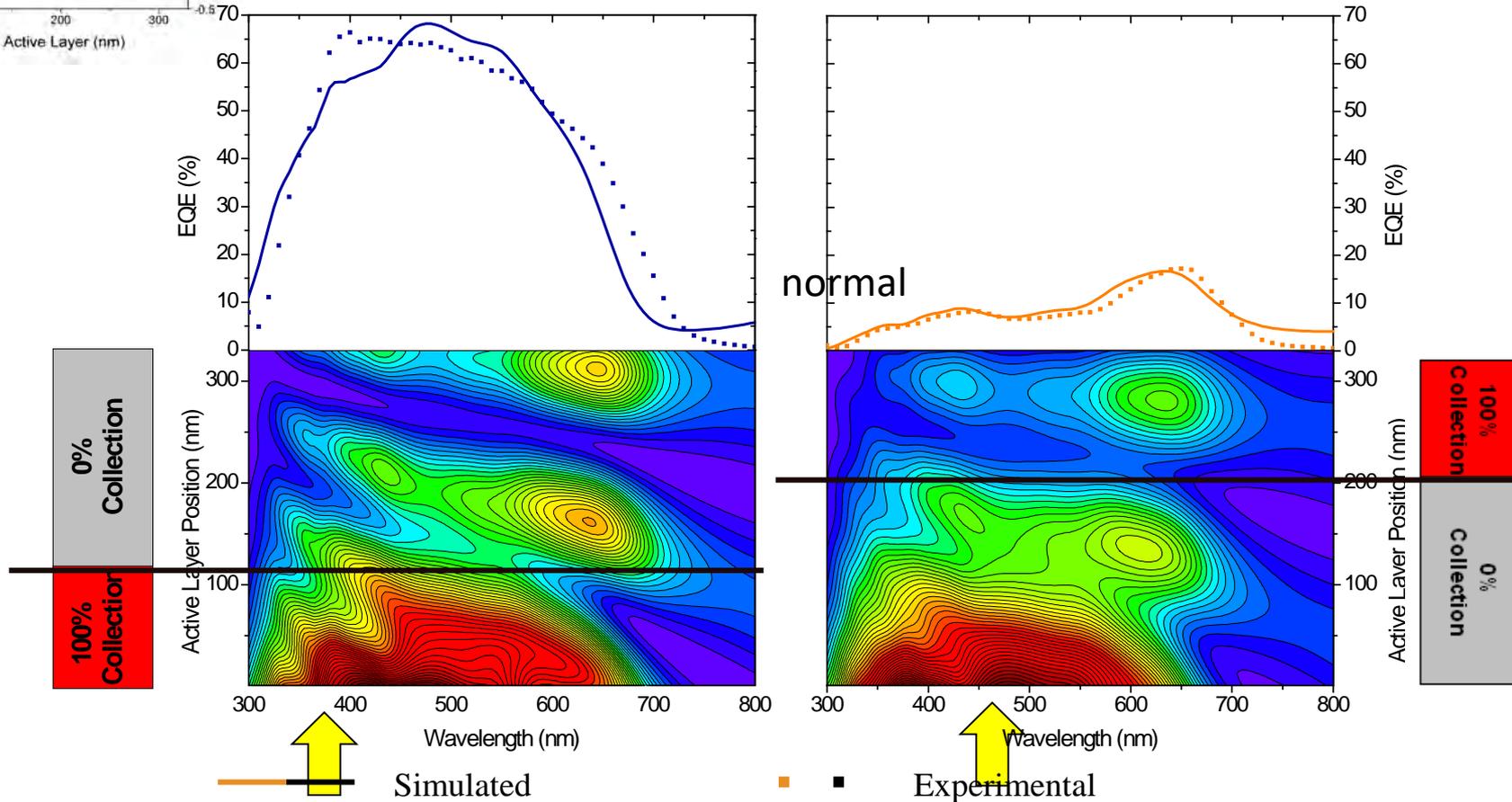
Case study I: Effect of unintentional doping



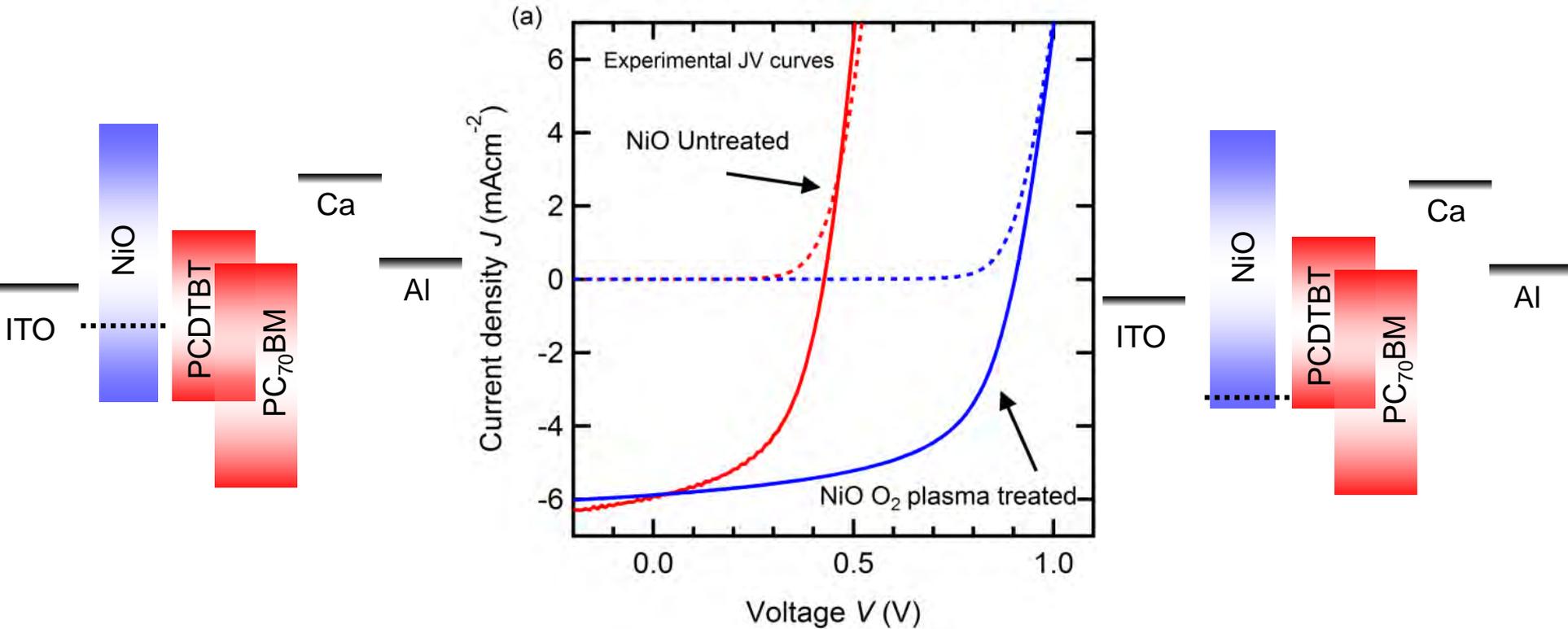
Current-voltage and EQE modelling serve as a diagnostic tool

Inverted

Standard

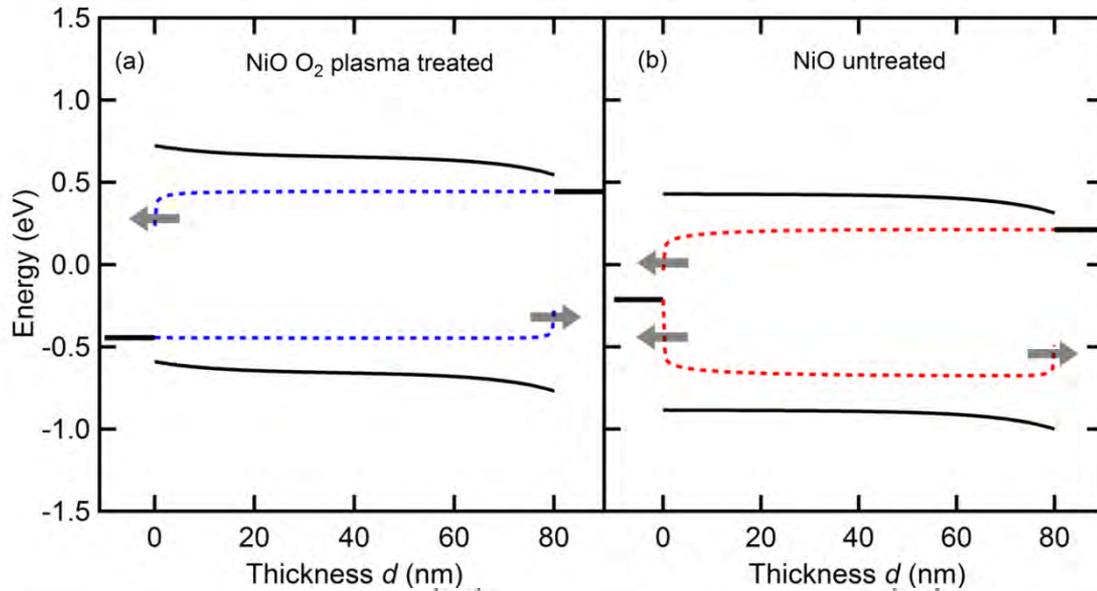


Case study II: electrode band alignment controls surface recombination and Voc



Oxygen plasma treatment of NiO interlayer leads to an increase in the open-circuit voltage

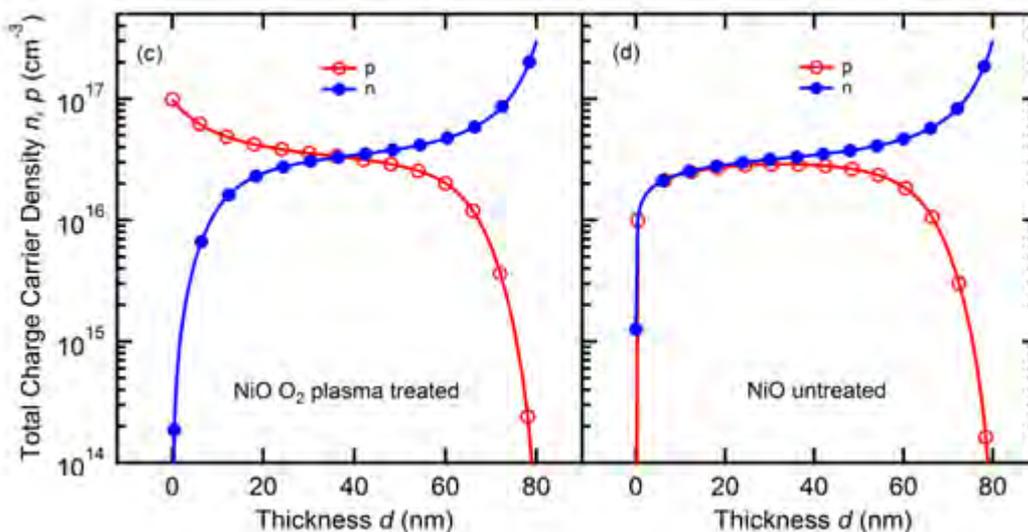
Case study II : electrode band alignment controls surface recombination and Voc



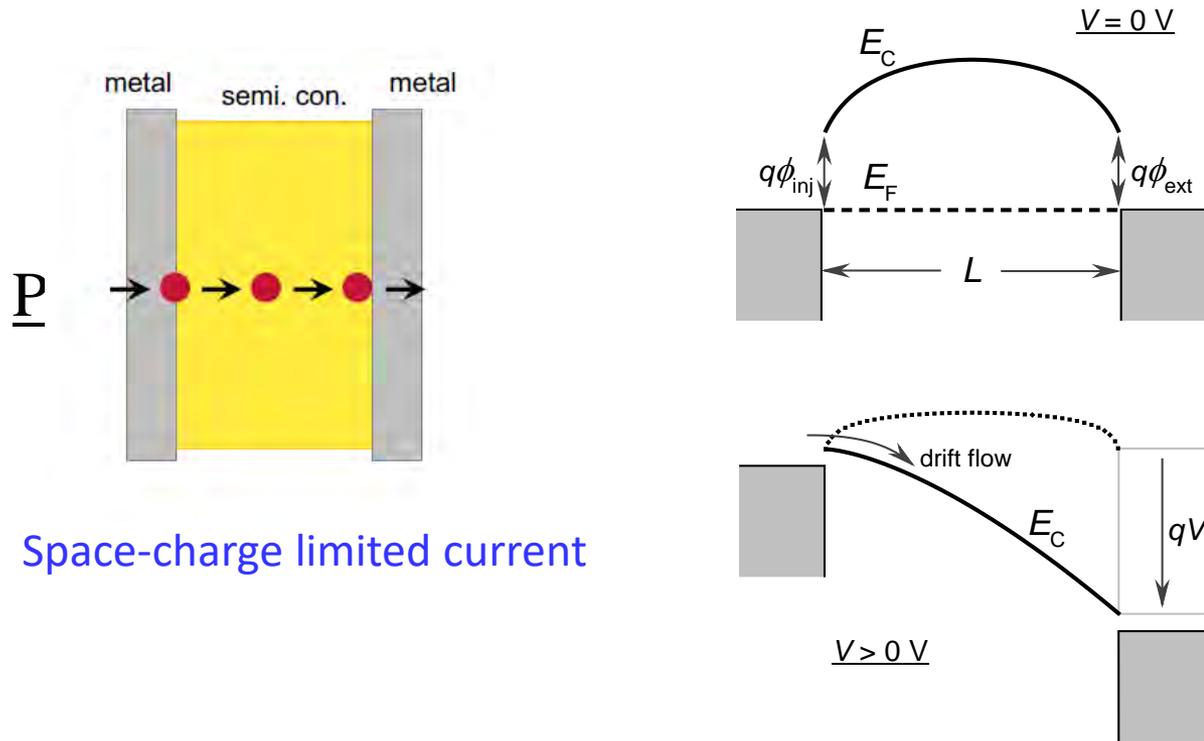
Quasi-Fermi level splitting in the bulk of the active layer largely unchanged

Gradient in the hole quasi Fermi-level at the anode indicates presence of surface recombination

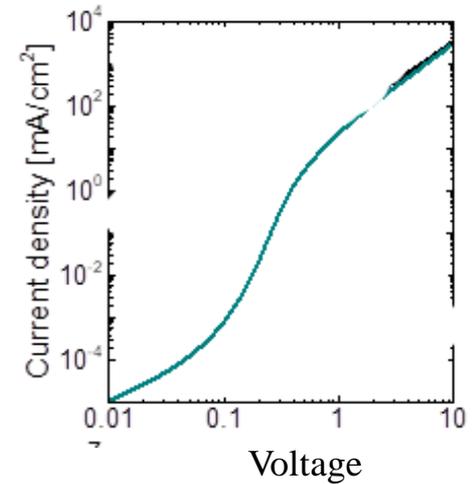
Surface recombination reduces Voc



III: Modelling space-charge-limited current measurements



Space-charge limited current

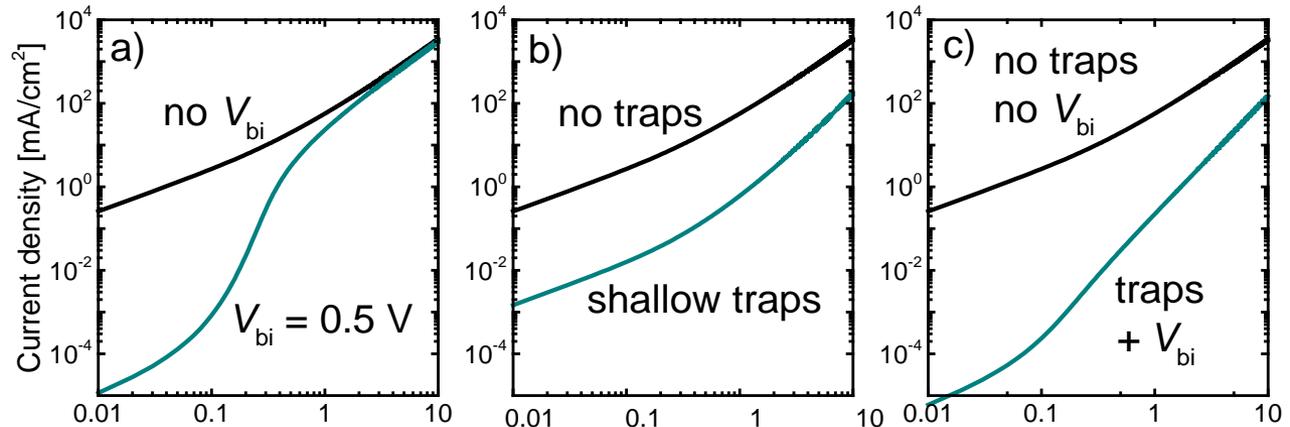


- Simple steady state dark current measurement commonly used to extract mobility
- In absence of traps or barriers, mobility is taken from Mott Gurney law $J = \frac{9}{8} \epsilon_0 \epsilon_r \mu \frac{V^2}{d^3}$

III: Modelling space-charge-limited current measurements

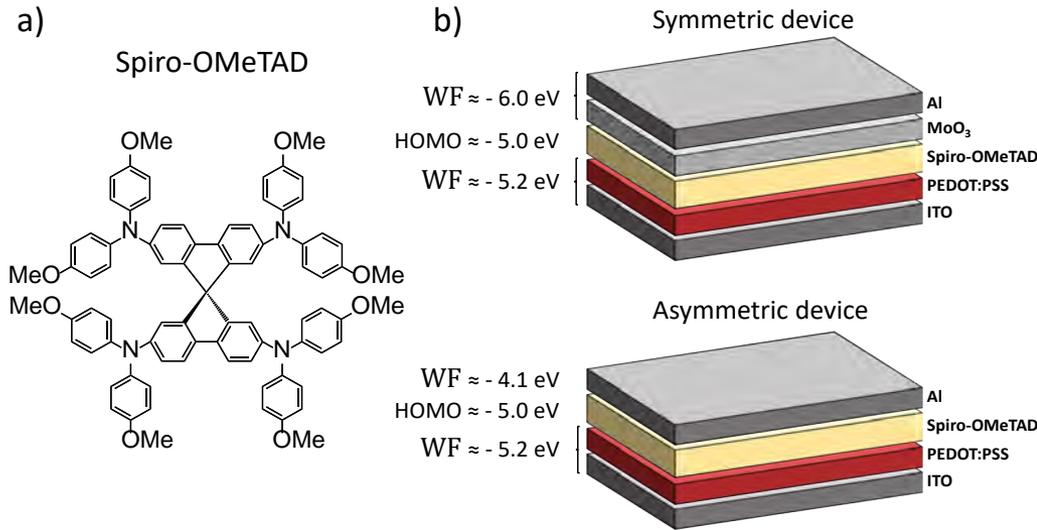
Mott Gurney law is seldom valid in practical cases. Need a numerical device model

J-V curves



- Solve semiconductor device equations in dark
- Introduce traps and / or tail states, Introduce injection barriers and / or V_{bi}

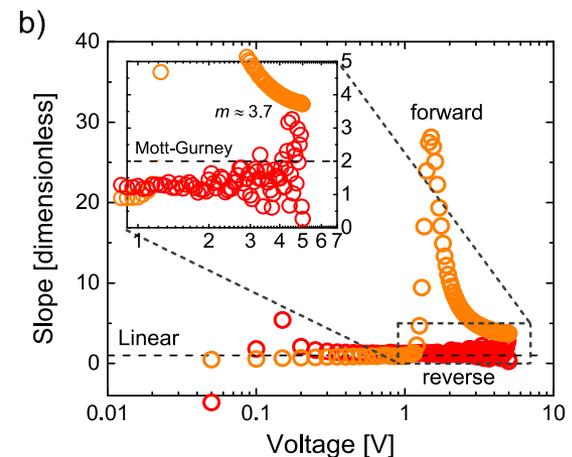
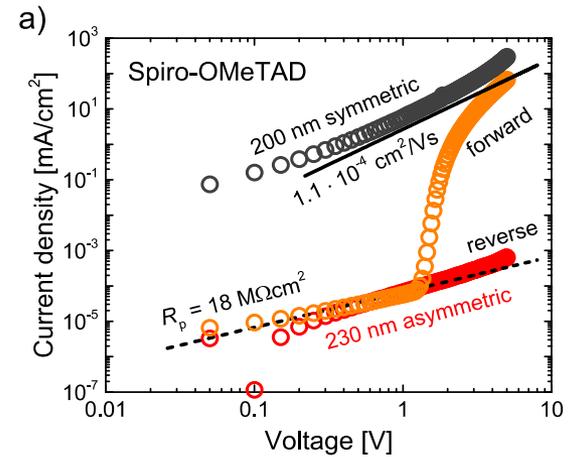
III: Modelling SCLC measurements in Spiro-OMeTAD



Fit with Mott Gurney $\Rightarrow \mu_h \approx 1 \times 10^{-4} \text{ cm}^2/\text{Vs}$

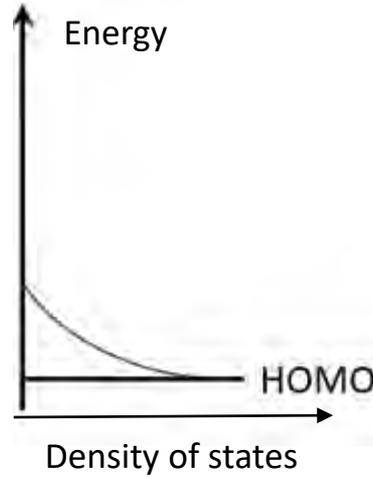
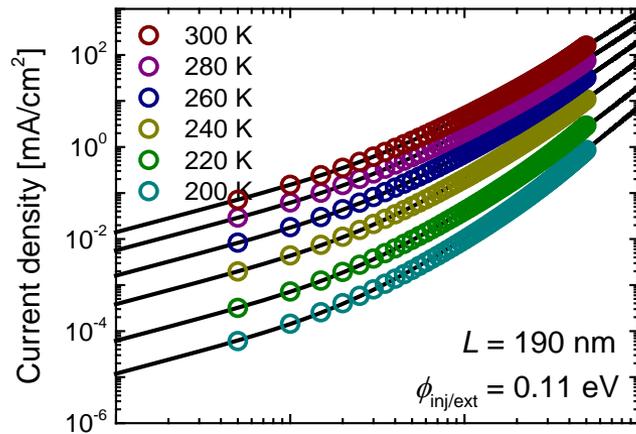
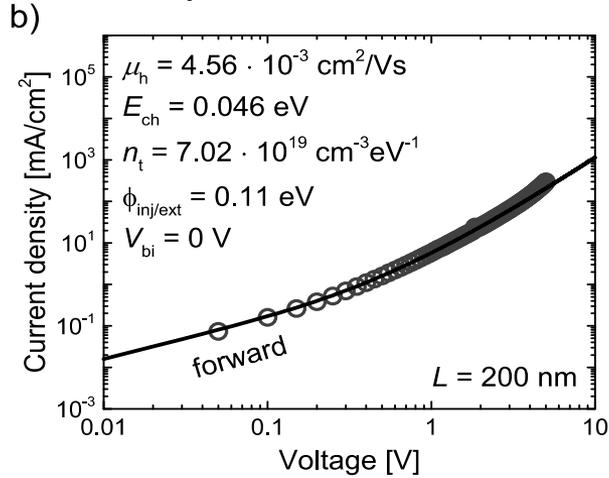
Consistent with previous reports

Is it reliable?

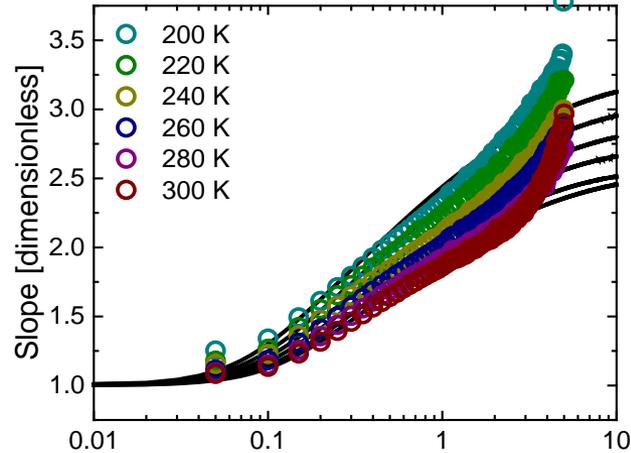
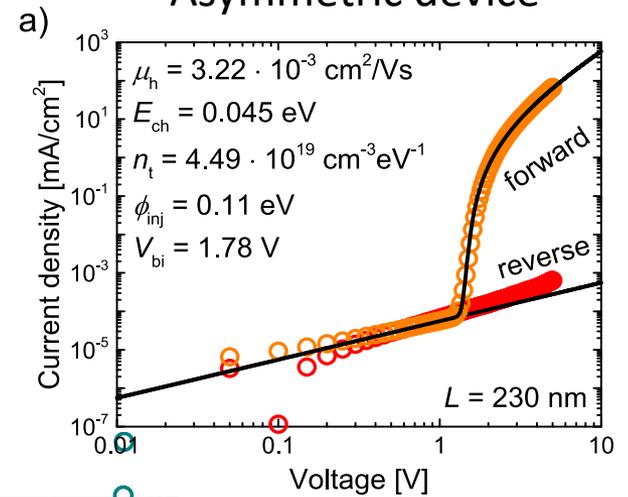


III: Modelling SCLC measurements in Spiro-OMeTAD

Symmetric device

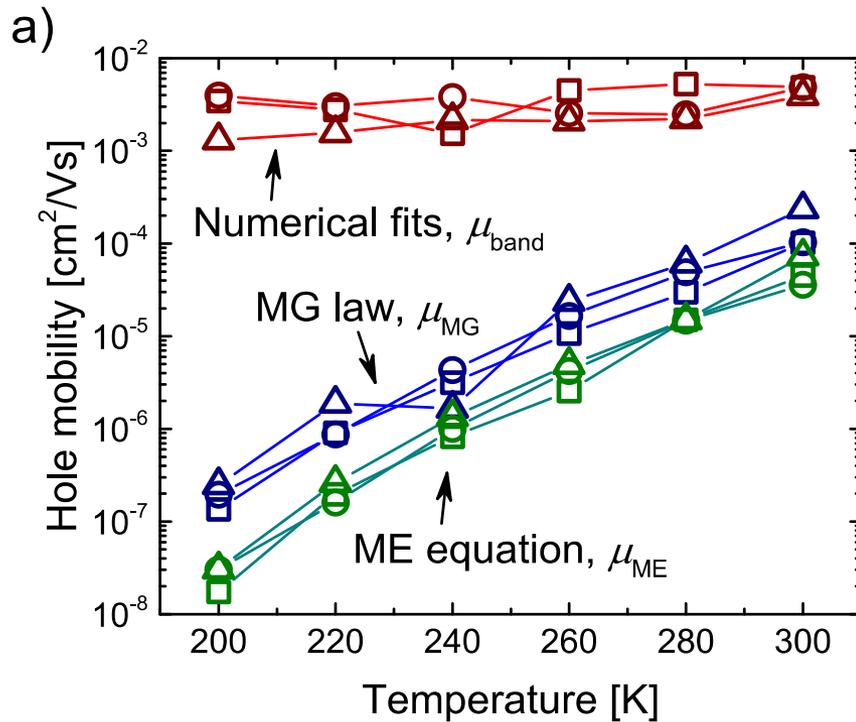


Asymmetric device



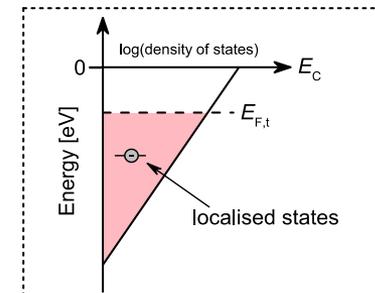
- Fit experimental data with numerical model including exponential tail of states
- Symmetric and asymmetric device data yield very similar models for DoS
- Temperature dependent data fit to same DoS

III: Modelling SCLC measurements in Spiro-OMeTAD



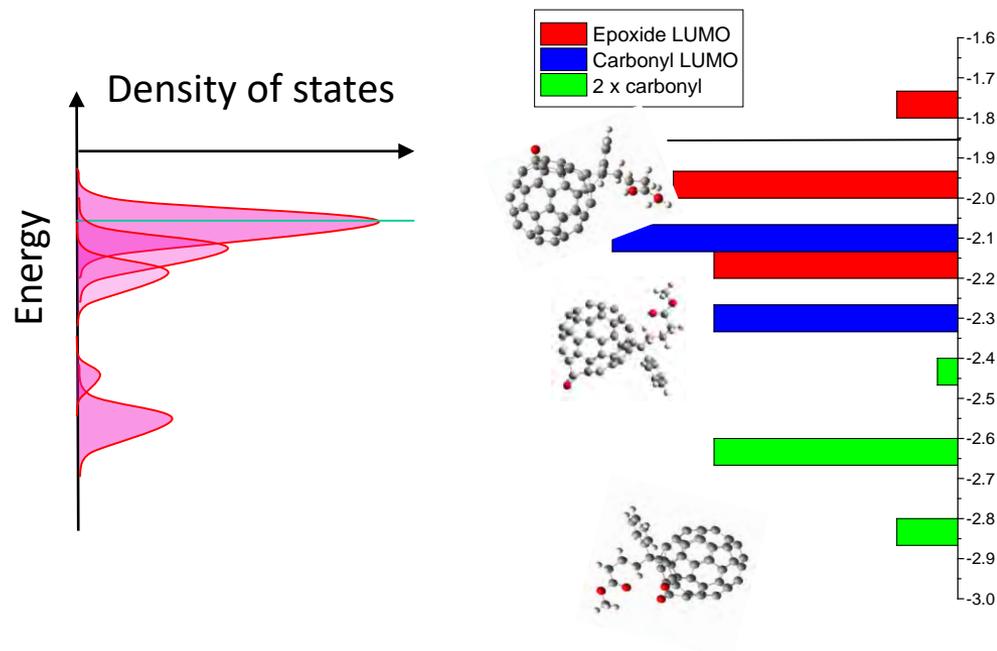
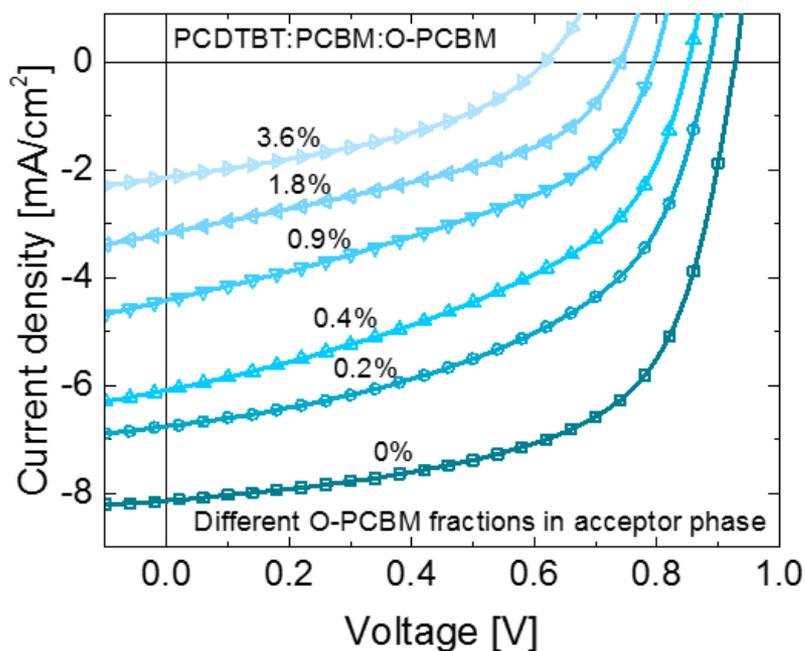
- Mott-Gurney law and moving electrode equation yield temperature dependent mobilities. Function of trapping and injection barriers..
- Numerical model yields a temperature independent *band* mobility...
- Validation for the transport model (trapped charge immobile, free charges have constant mobility)

c)



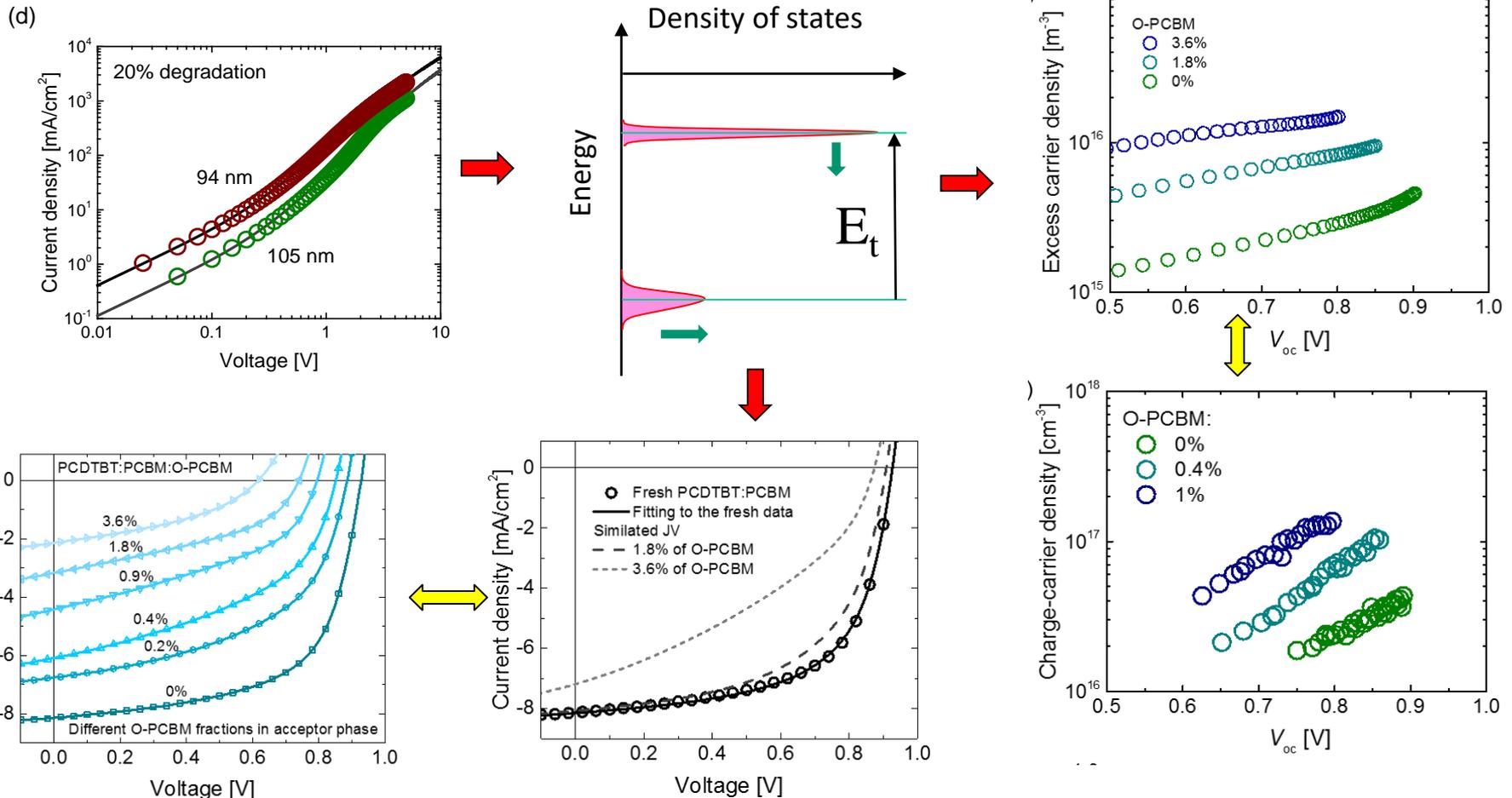
IV: Modelling electrical response of degraded OPV device

- Adding controlled amounts of oxidised fullerene reduces Voc, Jsc and fill factor
- Fullerene oxidation expected to induce **electron traps**
 - Likely to affect mobility, lifetime and density of states
- Can these explain the changes in device performance?



IV: Modelling electrical response of degraded OPV device:

- Modelling strategy:
 - SCLC \Rightarrow Deliver model for the density of states
 - Check against measured density of states from charge extraction
 - Apply to simulate device J-V response



Outline

- Basics of solar cell device modelling
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- Device modelling approaches to OPV
- Case studies: steady state models
- **Transient device modelling**

Beyond the simple device model: time resolved response

Drifffusion

An open source MATLAB-based drift diffusion simulation tool for modelling optoelectronic devices with mixed ionic-electronic semi-conductors

Download and contribute

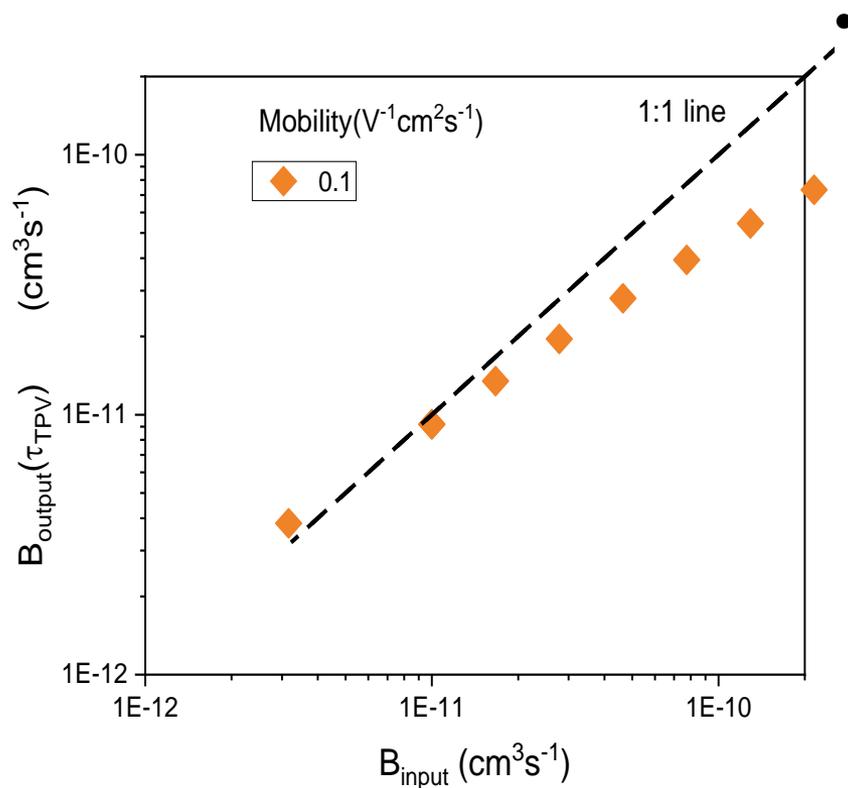
at: <https://github.com/barnesgroupICL/Drifffusion>

**Imperial College
London**

EPSRC

Engineering and Physical Sciences
Research Council

TPV and Recombination rate coefficient correlation



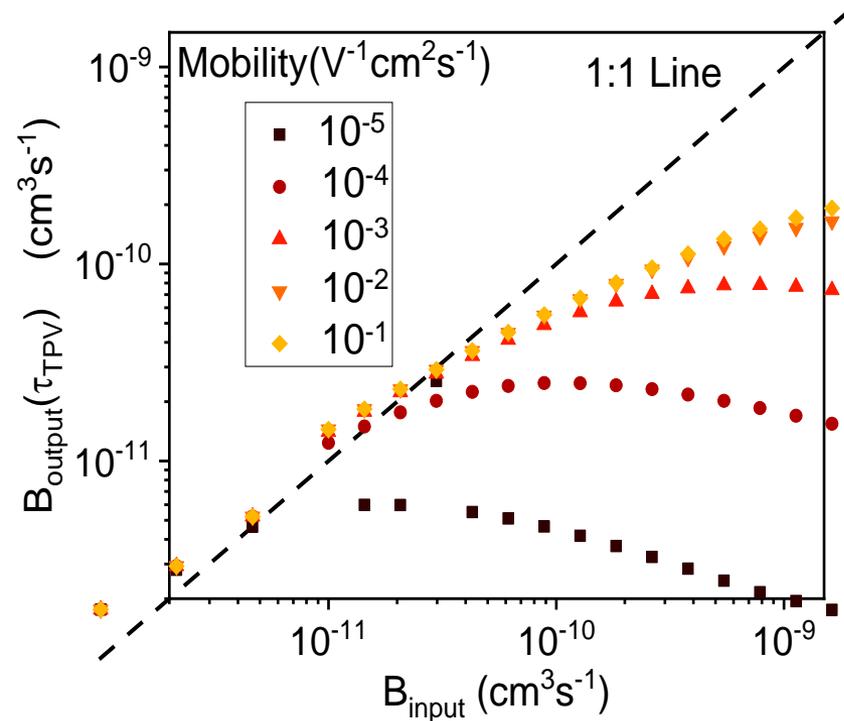
In the small perturbation approach ($\Delta n \ll n_{Voc}$):

$$B_{output}(\tau_{TPV}) = \frac{1}{2\tau_{TPV}n_{Voc}} \sim B_{input} \quad ?$$

n_{Voc} : is the excess charge in the device at open circuit under light intensity.

For High mobility devices and slow recombination the TPV lifetime is as expected

TPV and Recombination rate coefficient correlation



- In the small perturbation approach ($\Delta n \ll n_{Voc}$):

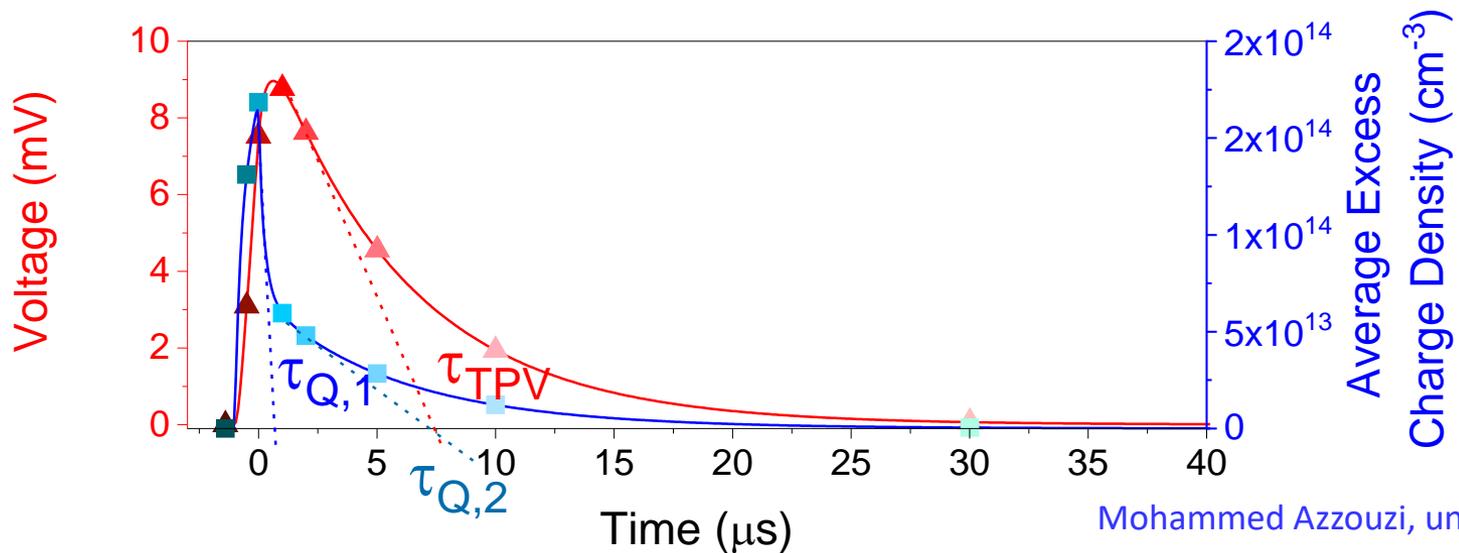
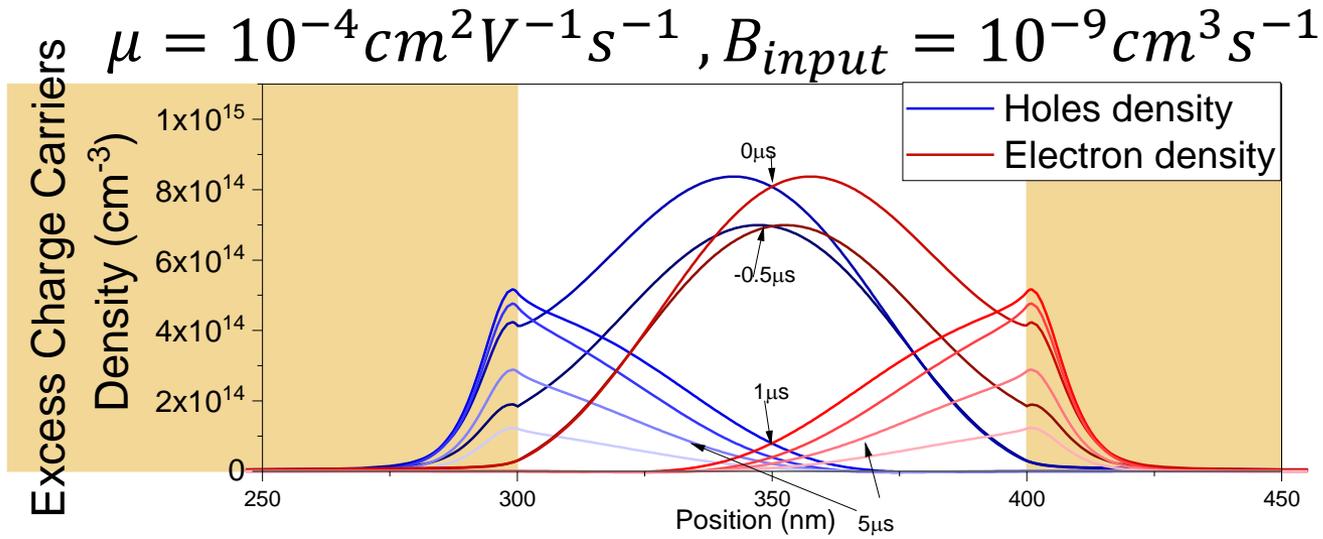
$$B_{output}(\tau_{TPV}) = \frac{1}{2\tau_{TPV}n_{Voc}} \sim B_{input} \quad ?$$

n_{Voc} : is the excess charge in the device at open circuit under light intensity.

For Low Mobility devices the recombination rates extracted from TPV deviate from the expected value



Simulated TPV Decay Differs from charge decay for low mobility or fast recombination



Why is the TPV Decay Different from the charge decay?

$$u = 10^{-4} \text{cm}^2 \text{V}^{-1} \text{s}^{-1}, B_{\text{input}} = 10^{-9} \text{cm}^3 \text{s}^{-1}$$



Do we need energy resolved device models?

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gpvdm

General-purpose Photovoltaic Device Model

[DOWNLOAD](#)

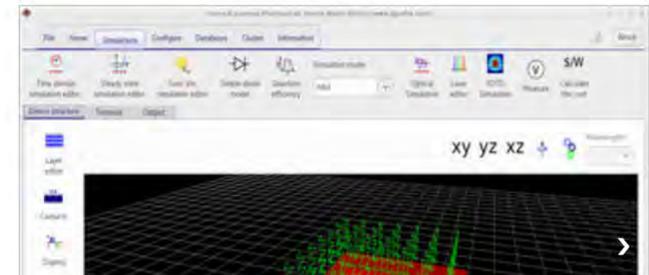
1 | **Monte Carlo Simulation - MC FLO** Perform easily Monte Carlo Simulations in Excel and make better decisions. mcflosim.ch

2 | **Materials Square - DFT/MD Simulation on demand** Start your DFT/MD simulation on the web right now! materialssquare.com

Simulate organic/Perovskite, Solar Cells, OFETs, and OLEDs for free!

gpvdm is a cross-platform opto-electronic device simulation tool. It can simulate **organic solar cells**, [OFET](#), [OLEDs](#), [Perovskite solar cells](#), and many other types of 1st, 2nd and 3rd generation solar cells. It contains both electrical model and optical models to produce accurate and predictive device simulations. The model can simulate the following types of devices out of the box:

- Organic solar cells (OPV devices)
- Perovskite solar cells - devices with mobile ions
- Organic LEDs (OLEDs)
- Organic Field Effect Transistors (OFETs)
- Crystalline silicon solar cells



www.gpvdm.com

Dr Rod MacKenzie, Nottingham University

Beyond the simple device model: energy resolved carriers

Gauss's Law

$$\nabla \epsilon_o \epsilon_r \cdot \nabla \phi = q \cdot (n - p)$$

Current driving terms

$$J_n = q \mu_e n \nabla E_c + q D_n \nabla n$$

$$J_p = q \mu_h p \nabla E_v - q D_p \nabla p$$

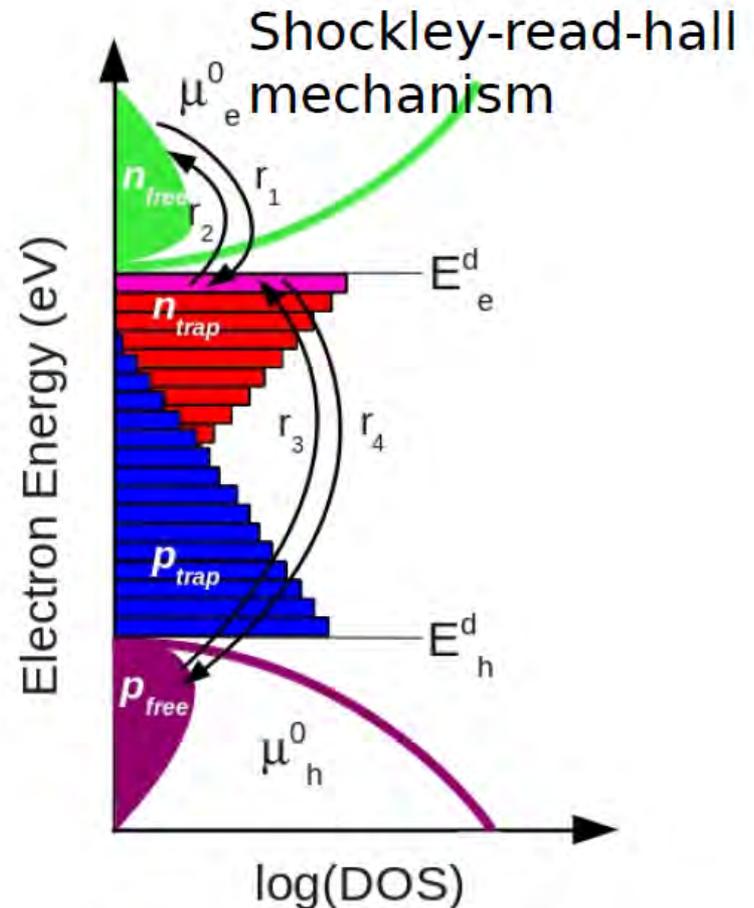
Current continuity equations

Electron continuity

$$\nabla \cdot \mathbf{J}_n = q \cdot \left(\sum_0^{n_{band}} (r_1^e - r_2^e) + \sum_0^{p_{band}} (r_3^h - r_4^h) + \frac{\partial n_{free}}{\partial t} \right)$$

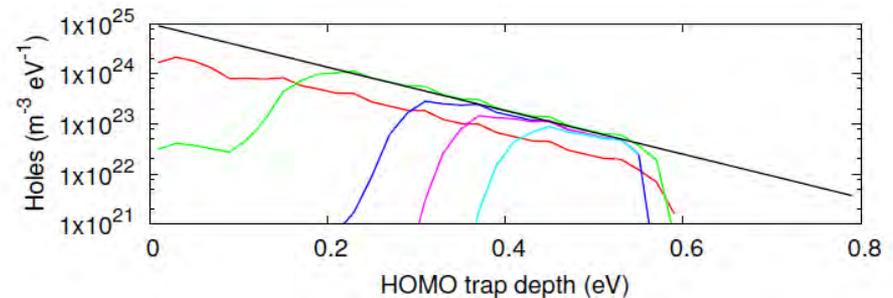
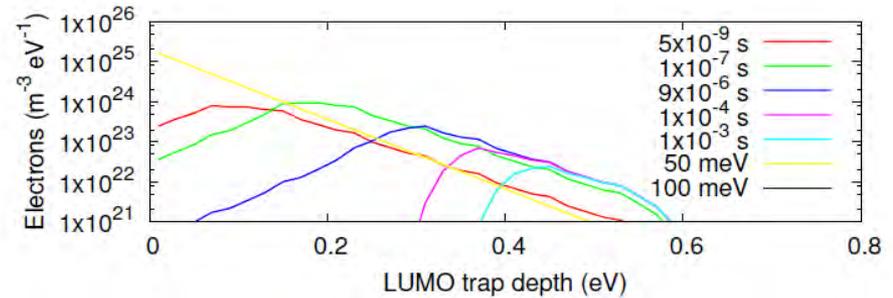
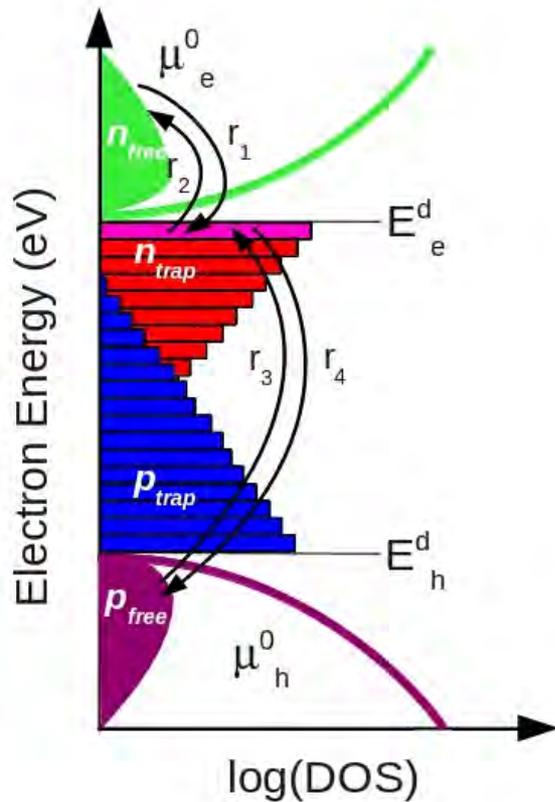
Hole continuity

$$\nabla \cdot \mathbf{J}_p = -q \cdot \left(\sum_0^{n_{band}} (r_3^e - r_4^e) + \sum_0^{p_{band}} (r_1^h - r_2^h) + \frac{\partial p_{free}}{\partial t} \right)$$



Do we need energy resolved device models?

- Model allows to track the energy distributions of charges during transients
- Thermalisation appears to occur on comparable time scales to charge dynamics
- **Penalty for energetic disorder may be less severe than expected from shape of DoS!**



Need experimental methods to probe charge energy distribution

Summary

- By making several simplifications (e.g. effective medium) OPV devices are modelled in steady state using traditional semiconductor device model approaches
- Important to include
 - sub-gap states (and recombination involving them)
 - (unintentional) doping
 - Interface barriers
 - Optical interference (sometimes)
- Most models do not include validated physical model for recombination coefficients or charge separation efficiency : these will be important when including spin dependent effects
- Transient models are sometimes necessary to relate observations to underlying physics